Eradicating infectious disease using weakly transmissible vaccines

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Viral vaccines have had remarkable positive impacts on human health as well as the health of domestic animal populations. Despite impressive vaccine successes, however, many infectious diseases cannot yet be efficiently controlled or eradicated through vaccination, often because it is impossible to vaccinate a sufficient proportion of the population. Recent advances in molecular biology suggest that the centuries-old method of individual-based vaccine delivery may be on the cusp of a major revolution. Specifically, genetic engineering brings to life the possibility of a live, transmissible vaccine. Unfortunately, releasing a highly transmissible vaccine poses substantial evolutionary risks, including reversion to high virulence as has been documented for the oral polio vaccine. An alternative, and far safer approach, is to rely on genetically engineered and weakly transmissible vaccines that have reduced scope for evolutionary reversion. Here, we use mathematical models to evaluate the potential efficacy of such weakly transmissible vaccines. Our results demonstrate that vaccines with even a modest ability to transmit can significantly lower the incidence of infectious disease and facilitate eradication efforts. Consequently, weakly transmissible vaccines could provide an important tool for controlling infectious disease in wild and domestic animal populations and for reducing the risks of emerging infectious disease in humans.

1. Introduction

The development of viral vaccines has had remarkable and long-lasting impacts on human health and on the health of domestic and wild animal populations. For instance, viral vaccines have been instrumental in the worldwide eradication of smallpox and rinderpest, the elimination of polio within much of the developed world, and the effective control of many other diseases [1–4]. Despite these impressive successes, many infectious diseases cannot yet be efficiently controlled or eradicated through vaccination programmes, either because an effective vaccine has not yet been developed (as with HIV) or because it is impossible to vaccinate a sufficient proportion of the population to guarantee herd immunity [5]. This problem is particularly acute for diseases of wildlife, including emerging infectious diseases such as Ebola, Middle East respiratory syndrome (MERS) and rabies where direct vaccination is impractical, cost-prohibitive or even impossible [6].

Recent advances in molecular biology suggest that the centuries-old method of individual-based vaccine delivery could be on the cusp of a major revolution. Specifically, genetic engineering brings to life the possibility of a transmissible or ‘self-disseminating’ vaccine [6,7]. Rather than directly vaccinating every individual within a population, a transmissible vaccine would allow large swaths of
the population to be vaccinated effortlessly by releasing an infectious agent genetically engineered to be benign yet infectious. This concept may sound like science fiction, but the oral polio vaccine already does this to a limited extent [8], and transmissible vaccines have now been developed and deployed in wild animal populations [6]. For instance, recombinant transmissible vaccines have been developed to protect wild rabbit populations against myxomatosis [9] and to interrupt the transmission of Sin Nombre hantavirus in reservoir populations of deer mice [10,11]. In addition, a transmissible vaccine is currently being developed to control Ebola within wildlife reservoirs [12]. Given the current pace of technological advance in genetic engineering, it is only a matter of time before transmissible vaccines can be easily developed for a wide range of infectious diseases.

Although promising, transmissible vaccines are not without risks. The most obvious and significant risk posed by a live transmissible vaccine is the potential for increased virulence to evolve. For instance, if a transmissible vaccine is developed through attenuation involving only a few genetic substitutions, reversions to wild-type virulence may evolve rapidly, as has occurred repeatedly with the oral polio vaccine [8,13]. The risk of reversion to high virulence can be minimized by genetically engineering transmissible vaccines using techniques that impede evolution, such as inflicting a large number of mildly deleterious mutations, rearranging the genome or imposing deletions [7]. Still, even the best engineered transmissible vaccines may ultimately evolve elevated virulence if sufficiently long chains of transmission are allowed to occur. Thus, the safest implementation would also engineer the vaccine so that it can transmit only weakly (R0 < 1), such that chains of transmission are short and stutter to extinction without continuous reintroduction. Transmissible vaccines designed in this way would be much less likely to evolve increased virulence or self-sustaining epidemics [14]. What remains unknown, however, is whether these safe but only weakly transmissible vaccines would significantly enhance our ability to control and eradicate infectious disease.

Here, we develop and analyse a mathematical model that allows us to quantify the extent to which a transmissible vaccine could facilitate efforts to eradicate infectious disease. Although our results apply to vaccines with arbitrary transmission rates, we will focus primarily on weakly transmissible vaccines (R0 < 1). This is because these represent the safest implementation. Our model is a straightforward extension of existing models of direct vaccination, differing only by including the potential for vaccine transmission among hosts. We use our model to answer two specific questions. First, how much does vaccine transmission facilitate disease eradication? Second, when eradication is impossible, how much does vaccine transmission reduce the incidence of infectious disease within the host population? Answering these questions provides an important first step in quantifying the potential gains that could accrue through the use of a transmissible vaccine.

2. The model

Our model assumes populations are large and well mixed, allowing us to capitalize on the well-developed SIR modeling framework [5]. Specifically, we assume hosts are either susceptible to the disease and vaccine (S), infected by the vaccine (V), infected by the disease (W) or immune/resistant to both vaccine and disease (R). Individuals are assumed to be born at a constant rate, b, which is independent of population size. A constant fraction of these newborn individuals, σ, are assumed to be vaccinated directly. Individuals infected with the disease independently transmit the disease to susceptible individuals at rate, βν, and recover and become immune at rate, δν. Individuals infected with the disease transmit the disease to susceptible individuals at rate, βW, recover and become immune at rate, δW, and succumb to the disease at rate, v. Individuals in all classes are assumed to die at a constant background rate, d. Together, these assumptions lead to the following system of differential equations:

\[
\begin{align*}
\frac{dS}{dt} &= b(1 - \sigma) - \beta_V SV - \beta_W SW - dS, \\
\frac{dV}{dt} &= b\sigma + \beta_V SV - \delta_V V - dV, \\
\frac{dW}{dt} &= \beta_W SW - \delta_W W - (d + v)W, \\
\frac{dR}{dt} &= \delta_V V + \delta_W W - dR,
\end{align*}
\]

where all variables and parameters are described in table 1.

<table>
<thead>
<tr>
<th>parameter</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td>b</td>
<td>birth rate of susceptible individuals</td>
</tr>
<tr>
<td>σ</td>
<td>proportion of individuals directly vaccinated at birth</td>
</tr>
<tr>
<td>βν</td>
<td>rate of vaccine transmission</td>
</tr>
<tr>
<td>βW</td>
<td>rate of disease transmission</td>
</tr>
<tr>
<td>d</td>
<td>disease independent death rate of hosts</td>
</tr>
<tr>
<td>δν</td>
<td>recovery rate of vaccine infected individuals</td>
</tr>
<tr>
<td>δW</td>
<td>recovery rate of disease infected individuals</td>
</tr>
<tr>
<td>v</td>
<td>increase in death rate of infected hosts caused by disease</td>
</tr>
</tbody>
</table>

3. Mathematical analyses

Employing a transmissible vaccine could make it possible to eradicate infectious diseases that have been recalcitrant to direct vaccination alone, and could be particularly useful for eliminating disease in domestic and wild animal populations. We explored this possibility by solving for the conditions under which a transmissible vaccine drives an infectious disease to extinction. Specifically, results derived in appendix A reveal that the fractional reduction in the vaccination threshold arising from use of a transmissible vaccine is given by

\[
\frac{R_{0,V}}{R_{0,W}}
\]

where the quantities R0,W and R0,V are the basic reproductive numbers for the infectious disease and vaccine, respectively. Result (3.1) reveals that the extent to which vaccine transmission facilitates eradication efforts depends on the relative R0 values of vaccine and disease (figure 1). Thus, the closer the R0 of the vaccine to that of the disease, the greater the reduction in direct vaccination effort required for disease eradication. For the particular class of weakly transmissible vaccines we focus on here (i.e. R0,V < 1), this result suggests a transmissible vaccine will have its most appreciable (more than 10%)
impacts on the wide range of moderately infectious diseases with $R_{0,W} < 10$ (e.g. those shown in table 2). Additional analyses performed in the electronic supplementary materials demonstrate that this result remains unchanged even when vaccination is imperfect such that vaccinated individuals return to the susceptible state at some fixed rate.

Even in cases where a transmissible vaccine does not allow an infectious disease to be eradicated, it may still reduce disease incidence substantially. We investigated this possibility by solving for the equilibrium incidence of the infectious disease in the absence and presence of vaccine transmission. By comparing these equilibria, we were able to quantify the proportional reduction in disease incidence attributable to vaccine transmission:

$$f_{\text{incidence}} = \frac{\sigma R_{0,V} R_{0,W}}{(R_{0,V} - R_{0,W})(1 - R_{0,W}(1 - \sigma))},$$

(3.2)

where $\sigma$ is the fraction of newborns directly vaccinated and is less than the critical value guaranteeing disease eradication given by equation (A.5) (figure 2). The key implication of (3.2) is that even weakly transmissible vaccines can significantly reduce the incidence of an infectious disease, particularly in cases where the infectious disease is not excessively transmissible (e.g. those shown in table 2).

### 4. Simulations and numerical analyses

To evaluate the robustness of our analytical results to random variation in transmission, vaccination rate and population sizes, we conducted stochastic simulations of our model. Simulations used the Gillespie stochastic simulation algorithm [22] to study the probability of disease elimination with a transmissible vaccine. Simulations were run for three different vaccine transmission rates and initiated with the susceptible population at its disease and vaccine free equilibrium (1000 individuals) and an initial seed of 50 individuals infected with the wild-type disease; resistant hosts and vaccine infected hosts were initially absent. For each transmission rate, 1000 simulations were run for a 100-year burn-in period followed by introduction of a vaccination programme. Simulations were then run for an additional time period and the proportion of simulations in which the disease was eradicated recorded.

Additional simulations evaluated the probability of disease extinction as a function of vaccine $R_0$, by conducting 1000 replicate simulations for values of vaccine $R_0$ ranging from 0 to 1. These values of vaccine $R_0$ bracketed the critical value for disease eradication predicted by equation (A.5), and show that reductions in disease incidence caused by the transmissible vaccine result in a high probability of disease eradication even before the critical threshold of vaccine transmission is reached (figure 4). The reason disease eradication occurs prior to reaching the eradication threshold is that vaccine transmission reduces the number of individuals infected with the disease sufficiently for stochastic extinction to become likely.

Finally, to evaluate the sensitivity of a transmissible vaccine to reversion, we simulated a slightly modified model where

**Table 2. Examples of important diseases with small $R_0$.**

<table>
<thead>
<tr>
<th>disease</th>
<th>$R_0$</th>
<th>references</th>
</tr>
</thead>
<tbody>
<tr>
<td>rabies</td>
<td>&lt;2</td>
<td>[15]</td>
</tr>
<tr>
<td>bovine TB</td>
<td>&lt;2</td>
<td>[16,17]</td>
</tr>
<tr>
<td>avian influenza</td>
<td>&lt;3</td>
<td>[18,19]</td>
</tr>
<tr>
<td>foot and mouth disease</td>
<td>&lt;3</td>
<td>[20]</td>
</tr>
<tr>
<td>Ebola</td>
<td>&lt;2</td>
<td>[21]</td>
</tr>
</tbody>
</table>

Overall, the results of the simulation runs provided strong support for our analytical solutions. Specifically, under conditions where our analytical results predict a traditional, non-transmissible vaccine would fail to eradicate the disease, eradication occurred in only 2.4% of simulations (24 of 1000 simulations; figure 3a). By contrast, a modestly transmissible vaccine ($R_0 = 0.93$) resulted in the eradication of this disease in 99.9% of simulations (999 of 1000 simulations), in cases where our analytical results predicted eradication (figure 3c). In intermediate scenarios ($R_0 = 0.33$) where our analytical results predicted vaccine transmission would reduce infection rates but fail to completely eradicate the disease, simulations showed vaccine transmission reduced the number of infected individuals by 61.8% relative to a non-transmissible vaccine and resulted in disease eradication in 39.2% of simulations (392 of 1000 simulations; figure 3b).
individuals infected with the vaccine \((V)\) were converted to individuals infected with wild-type virus \((W)\) at a constant rate \(r\) (see the electronic supplementary material for details). Results of these simulations demonstrated that our qualitative result, that vaccine transmission facilitates disease eradication, is robust to reversion. Reversion does, however, reduce the benefits provided by vaccine transmission. Only when reversion becomes very frequent can vaccine transmission actually reduce the likelihood of disease eradication, and even then this only occurs for vaccines that transmit very, very weakly (electronic supplementary material, figure S1).

5. Discussion

Our results show that even a weakly transmissible vaccine can substantially facilitate efforts to control or eradicate infectious disease. There are two important consequences of this result. First, if it is impossible to directly vaccinate a sufficient fraction of a population for disease eradication, whether due to limitations of public health infrastructure or prohibitive cost, vaccine transmission can tip the balance in favour of eradication. Second, even modest amounts of vaccine transmission can substantially reduce the effort and cost required to achieve a target level of vaccination within a population. These results are important because they demonstrate that it may be feasible to engineer transmissible vaccines that are effective while maintaining the greater margin of safety that comes from being only weakly transmissible \((R_0 < 1)\).

Unfortunately, even a weakly transmissible vaccine has some potential to revert to wild-type virulence. This is particularly true for live, attenuated vaccines developed using traditional methods that adapted a virus to unnatural conditions in the hope that growth in the focal host would decline and pathogenesis would wane. Because these old methods were haphazard, vaccines developed in this way may require only a few genetic changes to revert to wild-type virulence, as has been observed for the oral polio vaccine [13]. Fortunately, recent developments in genetic engineering provide considerable improvements in attenuation methods and the promise of reduced scope for reversion. One especially promising method is attenuation by introducing many silent codon changes [7,23,24]. For reasons still not fully understood, some types of silent codon changes reduce fitness slightly, and when dozens to hundreds of such changes are combined in the same genome, fitness can be reduced to arbitrary levels. Del- etions and genome rearrangements have similar attenuating effects and also appear to be suitable for different degrees of attenuation. When combined with weak transmission, the reduced probability of reversion provided by the new genetic technologies may make development of safe transmissible vaccines feasible.

Even if it becomes possible to genetically engineer transmissible vaccines that have very low probabilities of reversion,
ethical and safety concerns will likely preclude using them directly within human populations except under extraordinary circumstances [25,26]. Instead, the real power of transmissible vaccines likely lies in their ability to improve vaccine coverage in populations of livestock and wildlife where direct vaccination of a significant proportion of the population is excessively costly or even impossible in many cases. Although transmissible vaccines have not yet been used in this capacity on a large scale, a recombinant transmissible vaccine has been developed to protect wild rabbit populations against myxomatosis [9] and to interrupt the transmission of Sin Nombre hantavirus in reservoir populations of deer mice [6]. Similar approaches could be used to develop transmissible vaccines against invasive wildlife diseases, such as West Nile virus [27], to protect threatened wildlife populations from infectious disease [28] or to eliminate diseases like rabies from wild reservoir populations. The models we have studied here are obvious simplifications designed to make a first-pass estimate at the potential benefits that may be realized by using weakly transmissible vaccines. There are, of course, many ways in which our models could be generalized to evaluate the more nuanced biology of real populations, including spatial structure [29–31], heterogeneities in host populations [32–37], imperfect vaccines [38,39] and the potential for vaccine and disease evolution [14,40,41]. Circumscribing the conditions under which transmissible vaccines will provide benefits that exceed their potential risks will ultimately require exploration of these additional complexities.

6. Conclusion

The potential for a transmissible or self-disseminating vaccine to facilitate efforts to control and eradicate infectious disease has long been appreciated [42], but the oral polio vaccine and vaccines designed for wildlife remain the only well-documented examples [1,6,8–12]. Much of the reticence surrounding the development of transmissible vaccines stems from the justifiable concern that the potential for evolutionary reversion to wild-type virulence outweighs their potential benefits. Our results show, however, that even weakly transmissible vaccines can facilitate disease eradication and reduce disease incidence. When combined with new developments in genomic engineering that facilitate the development of transmissible vaccines that cannot easily evolve to be self-sustaining [7], these results suggest weakly transmissible vaccines may provide a safe and effective tool in the battle against infectious disease.

Appendix A. Analyses of equilibria and local stability

Mathematical analyses of equation (2.1a–d) reveals three possible equilibria, only two of which exist. The first equilibrium is given by

\[
\begin{align*}
\mathcal{S} &= \frac{d + v + \delta_W}{\beta_W}, \\
\mathcal{W} &= \frac{-d}{\beta_W} + \frac{b - b_W}{d + v + \delta_W} \\
&\quad + \frac{b_W(b_W + d + \delta_W) + \beta_W(d + v + \delta_W)}{b_W(b_W + d + \delta_W) - \beta_W(d + v + \delta_W)} \\
\mathcal{V} &= \frac{b_W(b_W + d + \delta_W) - \beta_W(d + v + \delta_W)}{b_W(b_W + d + \delta_W)},
\end{align*}
\]

and the second equilibrium is given by

\[
\begin{align*}
\mathcal{S} &= \frac{d^2 + b\beta_V + d\delta_V - \sqrt{4bd\sigma\beta_V(d + \delta_V) + (b\beta_V - d(d + \delta_V))^2}}{2d\beta_V}, \\
\mathcal{W} &= 0, \\
\mathcal{V} &= \frac{-d^2 + b\beta_V - d\delta_V + \sqrt{4bd\sigma\beta_V(d + \delta_V) + (b\beta_V - d(d + \delta_V))^2}}{2\beta_V(d + \delta_V)}.
\end{align*}
\]

Local stability analyses of (A1) and (A2) reveal that the equilibrium where the infectious disease is extinct (A2) is stable if:

\[
\sigma > \frac{(-b_Wd + d(d + v + \delta_W))(\beta_Wd + d + \delta_W)}{b_Wd(d + \delta_W)}.
\]

When this stability condition holds, the alternative equilibrium where the infectious disease is present (A1) is locally unstable. If local stability condition (A3) does not hold, the situation reverses and only the equilibrium with a positive density of individuals infected by the disease is locally stable. Thus, condition (A3) is sufficient to completely predict the qualitative dynamics of this system.

Defining the basic reproductive numbers of the vaccine and disease in the standard way as

\[
R_{0,V} = \frac{b\beta_V}{d(d + \delta_V)}
\]

and

\[
R_{0,W} = \frac{b\beta_W}{d(d + v + \delta_W)},
\]

allows condition (A3) to be re-written in a more insightful form defining the critical level of direct vaccination required for disease eradication:

\[
\sigma_{crit} = \left(1 - \frac{R_{0,V}}{R_{0,W}}\right)\left(1 - \frac{1}{R_{0,W}}\right).
\]

In the absence of vaccine transmission, (A5) reduces to the classical expression for the critical fraction of a population that must be vaccinated directly for disease
eradication to occur
\[
\alpha_{\text{crit}} = \left(1 - \frac{R_0,W}{R_0,V}\right).
\]  
(A.6)  

To make the benefits of vaccine transmission more transparent, we calculate the percentage reduction in vaccination effort provided by a transmissible vaccine relative to a traditional, non-transmissible vaccine
\[
\frac{f_{\text{Eradicate}} = 1 - \frac{\alpha_{\text{crit}}}{\alpha_{\text{crit}}} = 1 - \frac{1 - R_0,W/R_0,V}{1 - 1/R_0,W}}{1 - 1/R_0,W}.
\]
(A.7)  

This is equation (3.1) of the text.

To quantify the reduction in disease incidence provided by vaccine transmission, we calculated the following quantity:
\[
f_{\text{Incidence}} = 1 - \frac{\hat{W}}{W},
\]
(A.8)

where \(W\) is the equilibrium incidence of the infectious disease when confronted with a transmissible vaccine (equation (A.1b) with \(\beta_V > 0\)), and \(\hat{W}\) is the equilibrium incidence of the infectious disease when confronted with a non-transmissible vaccine (equation (A.1b) with \(\beta_V = 0\)). Making use of the previous definitions for \(R_0,V\) and \(R_0,W\) allows expression (A.8) to be simplified to the more intuitive expression (3.2) in the main text.

References


