On optimal hierarchy of load-bearing biological materials

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Load-bearing biological materials such as shell, mineralized tendon and bone exhibit two to seven levels of structural hierarchy based on constituent materials (biominerals and proteins) of relatively poor mechanical properties. A key question that remains unanswered is what determines the number of hierarchical levels in these materials. Here we develop a quasi-self-similar hierarchical model to show that, depending on the mineral content, there exists an optimal level of structural hierarchy for maximal toughness of biocomposites. The predicted optimal levels of hierarchy and cooperative deformation across multiple structural levels are in excellent agreement with experimental observations.

Keywords: biomechanics; hierarchical material; quasi-self-similar; biomimetic; toughness; flaw tolerance

1. INTRODUCTION

Multi-level structural hierarchy, as can be observed in a wide range of systems from chromosome, protein, cell, tissue to organisms, seems to be a universal strategy selected by natural evolution for realizing various properties and functions [1–5]. Based on biominerals and proteins (mainly type I collagen), a variety of load-bearing biological materials, such as bone, tooth, shell, tendon and antler, have emerged from evolution with ordered hierarchical microstructures that current man-made materials cannot achieve, and with strength and toughness surpassing their constituent phases by orders of magnitude [6–9]. Much progress has been made over the past several decades on the structure–property relations of biological materials at nano-, micro- and macro-levels, as well as a number of hierarchical levels integrated together [10–12]. In spite of these developments, important questions remain unanswered: what determines the size scales and hierarchical levels in a load-bearing biological material? Should there be an optimal number of structural levels in such materials, or is it simply the more levels the better? These questions are of interest not only to biologists but also to materials scientists who have recently synthesized biomimetic materials with microstructures mimicking, and properties exceeding, their natural counterparts [13–15]. To understand the principle of structural hierarchy in load-bearing biological materials, here we develop a quasi-self-similar structure model to show that, depending on the mineral content, there exists an optimal level of structural hierarchy for maximal toughness of hierarchical materials.

Figure 1 shows the hierarchical composite structures of bone, mineralized tendon and shell with different mineral content (45% of volume fraction in bone, 15% in mineralized tendon and 95% in shell [6–9]). Bone is seen to exhibit seven levels of structural hierarchy [16,17], with striking self-similarity near the bottom levels of hierarchy (figure 1a). Mineralized tendon fibres have four levels of hierarchy (figure 1b) with highly ordered, self-similar structures at every level [18], while tendon has six levels of hierarchy [19,20]. By contrast, sea shells show 2–3 levels of lamellar structures (figure 1c), with different structures at different levels [21].

To obtain a comprehensive understanding of biological materials, it is particularly important to bridge observations and behaviours across several length scales [22]. So far, there have been only limited studies of biological structures from a global hierarchical point of view. For example, it has been shown that the two-scale surface roughness on a lotus leaf can be explained by a size limit owing to static pressure of liquid drops [23], that the three-level hierarchy of alpha-helix-based protein filaments can be attributed to their optimal strength and toughness [24], and that the three-level structural hierarchy on Gecko’s feet can be related to a size limit owing to fibre fracture [25]. For load-bearing biological materials, a previously developed self-similar hierarchical model [10,12] failed to explain experimentally measured strain values of bone at different hierarchical levels [11] as well as why these materials typically exhibit two to seven levels of hierarchy depending on the mineral content. Our present model addresses this gap between theory and experiments, and helps to reveal the basic principles of structural hierarchy of load-bearing biological materials.

2. DERIVATION OF MODEL

Here we develop a quasi-self-similar composite model (figure 2) that mimics the bottom levels of hierarchy in load-bearing biological materials (figure 1). In this model, each hierarchical level consists of slender hard inclusions aligned in a parallel staggered pattern in a soft matrix. The structure at the n-th level serves as reinforcing inclusions at the (n+1)-th level. Since evolution

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tends to adapt biological systems to fit their functions, it can be assumed that the hierarchical structures of load-bearing biological materials have been optimized for stiffness and toughness. In accordance with this hypothesis, a set of design principles listed below will be used to construct the quasi-self-similar structural hierarchy and to examine how the material properties vary with the number of hierarchical levels.

(a) Principle of flaw-tolerance
In order to maximize toughness, we assume that the hierarchy renders material insensitive to the pre-existing crack-like flaws, a property interpreted as the removal of stress concentration at failure \[8\]. The condition for hard inclusions at the \((n+1)\)-th level of hierarchy to remain flaw-tolerant in the presence of random crack-like flaws is that the characteristic width \(h_n\) should satisfy the criterion \([10,12,26]\)

\[
h_n \leq \frac{E_n \Gamma_n}{S_n^2}, \quad n = 0, 1, 2, \ldots, N,
\]

where \(E_n, S_n, \Gamma_n\) denote the Young’s modulus, strength and fracture energy at the \(n\)-th level. The basic material properties at the \(n = 0\) level are \(E_0 = E_m, S_0 = \sigma_m, \Gamma_0 = 2\gamma_m\) where \(E_m, \sigma_m, \gamma_m\) stand for Young’s modulus, strength and surface energy of the mineral, respectively. The higher level composite properties \((n = 1, 2, \ldots, N\) level) are calculated by the recursive formulae \(([10,12];\) also see electronic supplementary material, text A and figure S1)

\[
E_n = \left[ \frac{4(1 - \varphi_{n-1})}{G^p_{n-1} \varphi_{n-1}^2 \rho_{n-1}^2} + \frac{1}{\varphi_{n-1} E_{n-1}} \right]^{-1},
\]

\[
S_n = \frac{1}{2} \varphi_{n-1} \rho_{n-1} \Gamma_{n-1}^p\rho_{n-1}^2,
\]

and \(\Gamma_n = (1 - \varphi_{n-1}) h_{n-1} \rho_{n-1} \Gamma_{n-1}^p\rho_{n-1}^2\).
where \( \varphi^{-1} \) and \( \rho^{-1} \) represent the volume fraction and aspect ratio of hard inclusions, while \( G_p \), \( \vartheta_p \) and \( \Theta_p \) denote the shear modulus, strength and failure strain of matrix at the \( n \)-th level. A related, but slightly different, point of view is that equation (2.1) ensures maximum redundancy of microstructure so that old and damaged materials can be constantly removed and replaced with fresh and healthy materials while an animal is conducting its normal activities [27].

(b) Criteria of equal strength and efficient stress transfer

The criterion of equal-strength is to make soft matrix and hard reinforcements reach their corresponding strengths at the same time [8,28]. According to this criterion, the aspect ratio \( \rho_n = h_n / h_0 \) of hard inclusions at the \((n+1)\)-th level is determined as

\[
\rho_n = \frac{S_n}{\tau_n} = \frac{S_n}{\tau_n^*}, \quad n = 0, 1, 2, \ldots, N - 1,
\]

where \( S_n \) is the tensile strength of the inclusions and \( \tau_n^* \) is the shear strength of the matrix.

The aspect ratio also plays an important role in the stress transfer between neighbouring inclusions via shear deformation in the matrix. In particular, there exists a critical aspect ratio beyond which a constant shear stress cannot be maintained in the matrix [29–31]. To achieve efficient stress transfer, the aspect ratio should not exceed the following critical value [see appendix A for the derivation],

\[
\rho_n^{STC} = 2 \sqrt{\frac{1}{\varphi_n} \frac{2(1-\varphi_n)}{\varphi_n \tau_n^*/\Theta_n^*}}
\]

where \( \tau_n^* \) and \( \Theta_n^* \) are, respectively, the shear strength and failure shear strain of the matrix, while \( E_n \) and \( \varphi_n \) are Young’s modulus and volume fraction of hard inclusions at the \((n+1)\)-th level. A combined criterion for selecting the aspect ratio is thus

\[
\rho_n = \min \{ \rho_n^{ESC}, \rho_n^{STC} \}.
\]

(c) Limited selection of constituent materials

Naturally occurring biological materials are constrained by a limited selection of constituent materials available [5,14]. Bone essentially consists of carbonated hydroxyapatite mineral crystals embedded in a soft matrix made of predominantly type I collagen [32,33]. The type I collagen accounts for 85–90% of total protein mass in bone [32]. Based on this fact, we assume that the matrix is made of the same type of protein (i.e. type I collagen) at all hierarchical levels, i.e.

\[
\tau_n^* = \tau_p, \quad G_n^* = G_p, \quad \Theta_n^* = \Theta_p, \quad n = 0, 1, 2, \ldots, N - 1,
\]

where \( \tau_p \), \( G_p \) and \( \Theta_p \) denote the shear strength, shear modulus and failure shear strain of the soft matrix, respectively. In the electronic supplementary material, text B and figure S2, we will show that this assumption could be relaxed by including two different types of protein without altering the main conclusions of the model.

Constituent materials are distributed at different structural levels in the quasi-self-similar hierarchical material. The volume fraction of mineral, \( \Phi \), varies according to the relative importance of stiffness and toughness. Experiments have shown that the stiffness tends to rise while the toughness decreases with increasing mineral content, as in mineralized tendon (\( \Phi = 15\% \)), bone (\( \Phi = 45\% \)) and shell (\( \Phi = 95\% \)) [1,6,7,9,33,34]. This suggests that toughness becomes a more dominant property as the mineral content is reduced. So far, there exists little information on how the constituent materials are distributed at different hierarchical levels. A simplest assumption is that the volume fraction of hard inclusions remains fixed at all hierarchical levels [10,12],

\[
\varphi_n = \Phi^{1/N}, \quad n = 0, 1, 2, \ldots, N - 1.
\]

Note that this assumption can also be relaxed without affecting the main conclusions of the model (see electronic supplementary material, text C and figure S3).

The above principles allow the quasi-self-similar hierarchical material to be constructed following a bottom-up design route shown in figure 3. Once the material parameters for mineral and protein, \( E_{m0}, \sigma_{m0}, G_{m0}, \tau_m, \gamma_{m} \) and \( \Phi \) are known, the properties of a \( N \)-level hierarchical material can be systematically calculated.

3. RESULTS

Figure 4a–d plots the calculated properties of the quasi-self-similar hierarchical material as a function of the hierarchical level number \( N \). The results based on the equal-strength criterion are compared with those based on the combined criterion of equal strength and efficient stress transfer. In these calculations, we have taken material parameters to be those of mineralized tendon, \( \Phi = 0.15 \), \( \gamma_m = 1 \text{ J m}^{-2} \), \( E_m = 100 \text{ GPa} \), \( \sigma_m = E_m/30 \), \( G_p = E_m/1000 \), \( \tau_p = \sigma_m/100 \) and considered two values \( \Theta_p = 35\% \) and \( \Phi = 100\% \) for the failure shear strain of the matrix. Figure 4a plots the overall stiffness of the quasi-self-similar hierarchical material normalized by the Voigt upper bound of the composite. It is seen that the stiffness decreases as the hierarchical level number
N increases. Figure 4b shows that the strength of the hierarchical material drops by roughly a factor of 2 with each added level of hierarchy, decreasing by about one order of magnitude with four levels of hierarchy. Figure 4c plots the variation of toughness with the hierarchical level number N for different θbp, showing that the toughness first increases and then decreases with increasing number of hierarchical levels. Therefore, there exists an optimal number of hierarchy for maximum toughness. This optimal number is N = 4 for θbp = 35% and N = 6 for θbp = 100%, suggesting that the property of soft material plays an important role in determining the optimal number of hierarchical levels. Interestingly, the plots calculated from the equal-strength criterion are almost the same as those from the combined criterion of equal strength and efficient stress transfer up to the optimal level of hierarchy, at which the material simultaneously achieves equal strength and efficient stress transfer in the structure. Figure 4d suggests that the quasi-self-similar hierarchical material will not be able to remain flaw-tolerant beyond the optimal level. Generally, tougher soft matrices lead to higher material toughness and larger structure size with more hierarchical levels.

4. DISCUSSION

The results shown in figure 4 indicate that, depending on the mineral content, increasing the number of hierarchical levels tends to increase material toughness until the optimal level is reached; increasing the number of hierarchies beyond the optimal level leads to decreasing toughness. The reason for this behaviour is that structural hierarchy imposes two opposing effects on the material. First, it allows the stress and deformation to be optimally partitioned between the inclusions and matrix, leading to higher toughness. However, higher toughness comes at a cost of decreasing stiffness and strength at increasing hierarchy. The reason for this behaviour is that structural hierarchy enables two opposing effects on the material. First, it allows the stress and deformation to be optimally partitioned between the inclusions and matrix, leading to higher toughness. However, higher toughness comes at a cost of decreasing stiffness and strength at increasing hierarchy.

Table 1 lists the size and mechanical properties of the quasi-self-similar material at different hierarchical levels for θbp = 35% up to the optimal level N = 4. It can be seen that the characteristic size varies from tens of nanometres (h0 = 18 nm for mineral bits at the bottom level) to hundreds of micrometres for the mineralized tendon fibre, and structural hierarchy becomes increasingly less effective in elevating toughness and structure size as the optimal level is reached. The predicted size scales and the optimal level of hierarchy are consistent with the experimental observations [18–20]. The magnification of toughness up to the optimal level is achieved at the cost of decreasing stiffness and strength at increasing hierarchical levels, which is consistent with the experimental observations [11,35,36].

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Figure 4. Variations of (a) Young’s modulus, (b) strength, (c) toughness, and (d) size of an N-level quasi-self-similar hierarchical material. (a,b) Turquoise circles, equal-strength criterion; blue triangles, combined criterion, θbp = 35%; red squares, combined criterion, θbp = 100%. (c,d) Purple pentagons, equal strength criterion, θbp = 35%; turquoise circles, equal strength criterion, θbp = 100%; blue triangles, combined criterion, θbp = 35%; red squares, combined criterion, θbp = 100%.
To be for bone is 4–6 if the fracture strain of soft matrix is taken and shell. It can be seen that the optimal level of hierarchy predicted optimal structures for bone, mineralized tendon and shell. For shell, our analysis indicates that no hierarchical structure is necessary if the soft matrix fails at 4–6 levels of structural hierarchy is optimal if more resilient soft matrix with 35% is used. The predicted self-similar hierarchical model with 35% has seven levels of hierarchy [16,17]. This is deemed a reasonable agreement given that the structure of bone and shell have also been performed (see figure S2 and table S2).

Our model shows that the ratio between strains at adjacent hierarchical levels satisfies 1 = (σn/En) = (En/Em) × h0/hn-1. Figure 5 plots the strain ratios e0 : e2 for the first three hierarchical levels against the corresponding experimental data measured by Gupta et al. [11]. Under the present assumption of an identical soft matrix at all hierarchical levels, our model predicts 4 : 2 : 1 for the first three hierarchical levels against the experimental observations of load-bearing biological materials because of the assumption of geometrical self-similarity, which implicitly demands a limitless iteration of decreasing number of hierarchical levels from bone to mineralized tendon and shell is in agreement with the experimental observations.

Our present analysis indicates that the previously developed hierarchical model [10,12] failed to explain experimentally observed behaviours of load-bearing biological materials because of the assumption of geometrical self-similarity, which implicitly demands a limitless selection of ever weaker soft materials at higher hierarchical levels. By contrast, nature is constrained by a very limited selection of structural proteins (primarily collagen). Our present model recognizes this fact and therefore correctly predicts the key experimental observations, including that there exists an optimal level of structural hierarchy.

It is worth pointing out that human beings have been able to discover and develop many materials, notably various metals, metallic alloys, ceramics, plastics, as well as their composites, with performances significantly surpassing biological materials [14]. However, it is not difficult to realize that most of the man-made materials are not environmentally friendly and have not been developed with genuine concerns over their sustainability on the evolutionary timescale. By contrast, biological materials are based on relatively weak constituents such as minerals and proteins which are easily degradable, bio-compatible, pollution-free, recyclable and energy-efficient. These properties are essential for long-term sustainability in evolution, and can be expected to become increasingly important to human civilizations as we approach the limit of natural resources. Understanding the hierarchical design principles of biological materials can provide useful guidelines on developing bioinspired 'green materials' based on bio-degradable and energy-efficient, hence environmentally friendly, materials in the future.

<table>
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<tr>
<th>Level</th>
<th>n</th>
<th>h0/hn-1</th>
<th>h0/hn-1</th>
<th>p0</th>
<th>low/l0-1</th>
<th>E0/Em</th>
<th>Sn/sm</th>
<th>G0/Gm</th>
<th>D0/Gm</th>
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<td>1</td>
<td>—</td>
<td>—</td>
<td>7.14E + 01</td>
<td>—</td>
<td>1</td>
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<td>24.2</td>
<td>2.22E + 01</td>
<td>7.52</td>
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<tr>
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<td></td>
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<td>4.90</td>
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<td>5.90</td>
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<td>9.96E - 03</td>
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<tr>
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<td></td>
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<td>6.69E - 03</td>
<td>3.83E + 02</td>
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Table 1. The predicted size and properties at different hierarchical levels of the mineralized tendon fibre based on the quasi-self-similar hierarchical model with θp = 35%.

Figure 5. Plots of strain ratios e0 : e2 (red circles) and e1 : e2 (green squares) for the first three levels of hierarchy in mineralized tendon fibres against experimental data [11]. Error bars are standard errors of the mean. Solid lines, theoretical, one soft matrix; dotted lines, theoretical, two soft matrices.

Table 2. Predicted optimal levels of hierarchy versus experimental observations for various load-bearing biological materials.

<table>
<thead>
<tr>
<th>Biological Material</th>
<th>optimal N</th>
<th>θp (%)</th>
<th>θp (%)</th>
<th>Nth observed in nature</th>
</tr>
</thead>
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<tr>
<td>Bone</td>
<td>45</td>
<td>35</td>
<td>100</td>
<td>7</td>
</tr>
<tr>
<td>Mineralized tendon</td>
<td>15</td>
<td>4</td>
<td>6</td>
<td>4–6</td>
</tr>
<tr>
<td>Shell</td>
<td>95</td>
<td>1</td>
<td>4</td>
<td>2–3</td>
</tr>
</tbody>
</table>

1–4 levels of hierarchy are close to experimentally observed 2–3 levels in shells [21]. The predicted trend of decreasing number of hierarchical levels from bone to mineralized tendon and shell is in agreement with the experimental observations.

Our present analysis indicates that the previously developed hierarchical model [10,12] failed to explain experimentally observed behaviours of load-bearing biological materials because of the assumption of geometrical self-similarity, which implicitly demands a limitless selection of ever weaker soft materials at higher hierarchical levels. By contrast, nature is constrained by a very limited selection of structural proteins (primarily collagen). Our present model recognizes this fact and therefore correctly predicts the key experimental observations, including that there exists an optimal level of structural hierarchy.

It is worth pointing out that human beings have been able to discover and develop many materials, notably various metals, metallic alloys, ceramics, plastics, as well as their composites, with performances significantly surpassing biological materials [14]. However, it is not difficult to realize that most of the man-made materials are not environmentally friendly and have not been developed with genuine concerns over their sustainability on the evolutionary timescale. By contrast, biological materials are based on relatively weak constituents such as minerals and proteins which are easily degradable, bio-compatible, pollution-free, recyclable and energy-efficient. These properties are essential for long-term sustainability in evolution, and can be expected to become increasingly important to human civilizations as we approach the limit of natural resources. Understanding the hierarchical design principles of biological materials can provide useful guidelines on developing bioinspired 'green materials' based on bio-degradable and energy-efficient, hence environmentally friendly, materials in the future.
In summary, our work shows that the evolution of load-bearing biological materials may have been guided by a clear set of physical principles/rules. We have shown that the experimentally observed hierarchical structures in load-bearing biological materials can be understood based on a quasi-self-similar model of hierarchical composite material. In this model, we have adopted a number of design rules including flaw-tolerance, equal strength and efficient stress transfer, while recognizing the fact that there is only a limited selection of constituent materials in nature. Using typical parameters of biological materials, our analysis indicates that there exists an optimal number of hierarchical levels, hence an optimal hierarchical structure, for maximum material toughness. Within the optimal hierarchy, the characteristic size from the bottom to top structures varies from tens of nanometres to hundreds of micrometres. These predictions are all in agreement with the experimental observations. The ratio between strains at the bottom three levels of hierarchy shows quantitative agreement with the experimental measurements. The predicted trend of decreasing number of hierarchical levels from bone to mineralized tendon and shell is also consistent with experiments. Our model reveals a number of physical principles/rules for load-bearing biological materials, which may benefit the development of biomimetic ‘green’ materials that are not only endowed with superior mechanical properties but also biocompatible, degradable, environment-friendly and energy-efficient.

This work was supported by the A*STAR Visiting Investigator Program ‘Size Effects in Small Scale Materials’ hosted at the Institute of High Performance Computing in Singapore.

APPENDIX A. CRITICAL ASPECT RATIO FOR EFFICIENT STRESS TRANSFER

Efficient stress transfer plays a key role in all composite materials, and in particular depends on the aspect ratio of hard inclusions in biocomposites [30,31]. In the staggered composites, the soft protein matrix usually has relatively low Young’s modulus and yield stress but large capacity of plastic deformation. In considering stress transfer, we model it as an ideal plastic material, as shown in figure 6. Equilibrium equations for hard inclusions 1 and 2 in figure 6 can be written as

\[
\frac{d\sigma_1(x)}{dx} = \frac{2\sigma_n}{\tilde{h}_n E_n} \left( \frac{l_n}{2} - x \right) \tag{A1}
\]

and

\[
\frac{d\sigma_2(x)}{dx} = \frac{2\sigma_n}{\tilde{h}_n E_n} x, \tag{A2}
\]

respectively.

Subtracting equation (A1) from equation (A2) yields

\[
\frac{d(u_2 - u_1)}{dx} = \frac{2\sigma_n}{\tilde{h}_n E_n} \left( 2x - \frac{l_n}{2} \right). \tag{A3}
\]

The thickness of the soft matrix layer between neighbouring inclusions can be expressed in terms of the thickness \(h\) and volume fraction \(\varphi\) of hard inclusions as \((1 - \varphi_n)h_n/\varphi_n\). Hence, shear deformation in the soft layer can be derived by integrating equation (A3),

\[
\gamma(x) = \frac{\varphi_n(u_2 - u_1)}{(1 - \varphi_n)h_n} = \frac{2\varphi_n \tau_n}{(1 - \varphi_n)h_n^2 E_n} \left( x^2 - \frac{l_n}{2} x + C \right). \tag{A4}
\]

For efficient stress transfer, the following conditions must be satisfied:

\[
\min \gamma = \frac{2\varphi_n \tau_n^p}{(1 - \varphi_n)h_n^2 E_n} \left( - \frac{l_n^2}{16} + C \right) = 0, \tag{A5}
\]

when \(x = \frac{l_n}{4}\)

and

\[
\max \gamma = \frac{2\varphi_n \tau_n^p}{(1 - \varphi_n)h_n^2 E_n} \cdot C = \Theta_n^p, \tag{A6}
\]

when \(x = 0\) or \(x = \frac{l_n}{2}\).

Combing equations (A5) and (A6), the critical length for efficient stress transfer is determined as

\[
\rho_n^{\text{STC}} = 2h_n \sqrt{\frac{2(1 - \varphi_n) \Theta_n^p E_n}{\varphi_n \tau_n}}, \tag{A7}
\]

and consequently the critical aspect ratio as

\[
\rho_n^{\text{STC}} = 2 \sqrt{\frac{(1 - \varphi_n) E_n}{\varphi_n \tau_n^p}}. \tag{A8}
\]

Note that this result is based on a direct analysis of tension-shear structure and differs slightly from that of Chen et al. [31].

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