Universal scaling of production rates across mammalian lineages

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Over many millions of years of independent evolution, placental, marsupial and monotreme mammals have diverged conspicuously in physiology, life history and reproductive ecology. The differences in life histories are particularly striking. Compared with placentals, marsupials exhibit shorter pregnancy, smaller size of offspring at birth and longer period of lactation in the pouch. Monotremes also exhibit short pregnancy, but incubate embryos in eggs, followed by a long period of post-hatching lactation. Using a large sample of mammalian species, we show that, remarkably, despite their very different life histories, the scaling of production rates is statistically indistinguishable across mammalian lineages. Apparently all mammals are subject to the same fundamental metabolic constraints on productivity, because they share similar body designs, vascular systems and costs of producing new tissue.

Keywords: production; life history; metabolic ecology; placental; marsupial; monotreme

1. INTRODUCTION

The three lineages of mammals, placentals (eutherians), marsupials (metatherians) and monotremes (prototherians), diverged more than 100 Ma ago [1–3]. They diversified rapidly on different landmasses as the supercontinent Pangaea fragmented and drifted apart [4–9]. As a consequence of their independent evolution, the extant members of these lineages differ conspicuously in physiology, life history and reproductive ecology [10–12].

Metabolic rates of marsupials and monotremes are about 33 and 50 per cent lower, respectively, than placentals [13], and the differences in life history are dramatic (figure 1). Monotremes lay eggs; the stored energy reserves support embryonic development, and then the females supply milk to fuel growth from hatching to independence. Marsupials have a very short period of intrauterine embryonic development, are born at a small size and undeveloped state and then are protected and lactated in a pouch for a long period before they become independent [14]. By contrast, placentals have a more prolonged period of intrauterine embryonic development, are born at larger size and are nourished by lactation until they become independent.

A common feature of these seemingly divergent life histories is that the mother supplies all of the nutrition to rear offspring to independence [15]. The metabolic rate of the mother fuels the production of biomass, and this limits the ways in which life-history traits can trade off to meet energy and material requirements of offspring at different stages of development. Because the metabolic rate of the mother is highly constrained by body size (cf. [16–20]), many life-history traits correlate closely with adult body size, scaling allometrically following the form

\[ R = R_1 M^\beta, \]

where \( R \) is the trait of interest, \( R_1 \) is a taxon- and mass-specific normalization constant, \( M \) is adult body size and \( \beta \) is a scaling exponent. Metabolic scaling theory predicts \( \beta \approx 3/4 \) for whole-organism metabolic rates, \( \beta \approx 1/4 \) for biological times such as duration of pregnancy and lactation and lifespan and \( \beta \approx -1/4 \) for most biological rates such as ontogenetic and population growth rates and the rate of offspring production [16].

Mechanistically, rate of offspring production depends on the rate at which biomass can be produced by the mother. Productivity is constrained by the logistical problems of transporting key materials such as oxygen and nutrients around the body [21]. Because all mammals have similar body plans and energetic costs of producing biomass [22], we expect them to be subject to similar constraints on production. Mass-specific production rate, \( p \), can be estimated as the mean mass of offspring produced per year, normalized by adult body size (or the annual amount of biomass produced per unit of adult body size), so

\[ p = \frac{m_b}{m} l \cdot n, \]

where \( m \) is adult body mass, \( m_b \) is mass at birth, \( l \) is litter size and \( n \) is the number of litters per year [23]. In placental mammals, mass-specific production rate scales with an exponent between \(-1/4 \) and \(-1/3 \), similar to mass-specific metabolic rate [23]. There is considerable variation in production rate across different
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functional and taxonomic groups of eutherian mammals, but most of this variation is in the normalization constant, \( R_1 \); the exponents are relatively constant across these groups because production rates are highly constrained by body size according to equation (1.1) [23,24]. However, because placentals, marsupials and monotremes give birth to offspring of very different sizes and developmental stages, a better and more standardized measure of production substitutes mass at weaning, \( m_w \), the stage at which mothers cease direct investment of energy to offspring growth, for mass at birth. Indeed, figure 2a shows that while size of offspring at birth scales predictably with adult body size in all lineages, newborn placentals are both absolutely larger and scale more steeply with adult body size than marsupials or monotremes. However, figure 2b shows that weaning mass is remarkably predictable across all lineages of mammals. So, mass-specific production measured at weaning is

\[
p = \frac{m_w}{m} \cdot l \cdot n. \tag{1.3}
\]

We address the effects of pre-weaning mortality on this measure of mass-specific production later in the discussion. Because all mammals have similar body plans, vascular systems and costs of producing new tissue, we hypothesize that all mammals should produce biomass at an equivalent mass-specific rate despite the differences between lineages in the size and timing of the life-history stages.

Figure 1. Schematic of differences in timing of the life history in similar-sized monotremes, marsupials and placentals. Female body mass ca 1500 g.

Figure 2. Bivariate log–log plots of offspring body mass (a) at birth and (b) newly weaned as a function of adult mass in grams. All logs are log-base 10, all mass units are grams and the figure legend is the same for all figures. Filled grey circles, placental; dashed lines, placental OLS; filled black circles, marsupial; solid lines, marsupial OLS; open circles, monotreme.
2. METHODS

To evaluate these predictions and explore variation in allocation to reproduction across placentals, marsupials and monotremes, we compiled a life-history database for more than 4000 non-volant mammalian species from both primary and secondary published sources (for more details, see electronic supplementary material, table S1). For each species, we recorded neonate mass (g), mass at weaning (g), adult body size (g), gestation time (months), time to weaning (months), age at first reproduction (months), maximum lifespan (months), litter size and litter frequency (per year), where data were available. For the placentals and marsupials, we used ordinary least squares (OLS) regression, fitted to bivariate log–log plots, to quantify allometric scaling of these life-history traits in terms of equation (1.1). For the mass-specific production analyses, we first used OLS regressions to estimate slopes within lineages, and then we used a general linear model (GLM) to test for significant differences between the lineages. For the GLMs between lineages, we controlled for taxonomy by nesting order within lineage because body size is confounded by phylogeny. Within the placental lineage, there are 20 orders represented in our dataset, and in the marsupial lineage, there are 7 orders represented. There were only three monotreme species, and so we show their data in figures, but do not include them in statistical analyses. All statistical analyses were performed in MINITAB 15.0.

3. RESULTS

(a) Life-history times

Figure 3a–e shows variation in life-history times as a function of body mass, all plotted on logarithmic axes. Comparing marsupials and placentals: (i) gestation time is short and nearly invariant in marsupials, whereas it is substantially longer and increases significantly with body size in placentals, (ii) time to weaning is substantially longer in marsupials than in placentals, but scales similarly with size, (iii) total development time (the sum of gestation time and time to weaning) is longer in marsupials than in placentals, (iv) age at first reproduction is widely variable and overlaps greatly, but tends to be greater in small marsupials and to scale less steeply with body size than in placentals, and (v) maximum lifespan is similar across lineages and scales very similarly with mass (see table 1 for statistical results). Slopes generally are close to the predicted 1/4, except for gestation time and age of first reproduction in marsupials, which are shallower.
(b) Fecundity

Figure 4a,b shows variation in the different components of fecundity. Litter size (figure 4a) is highly variable and scales more steeply in marsupials than in placentals, and the number of litters per year (figure 4b) overlaps greatly between marsupials and placentals of small body size, but is approximately invariant with size in marsupials and scales negatively in placentals. We combine litter size and the number of litters per year to estimate annual fertility, \( F_0 \), by rearranging equation (1.2) so that \( F_0 = l \cdot n = p \cdot (m/m_0) \). Figure 4c shows that for both placentals and marsupials, annual fecundity scales similarly, and close to \(-1/4\) power. So, despite the very different allocations to litter size and frequency, the number of offspring produced per year is identical across lineages, but the relationship is not tight in either group. Further, lifetime fertility, \( F_L \), is annual fertility \( \times \) adult lifespan, \( a \), or \( F_L = a \cdot p \cdot (m/m_0) \) (where adult lifespan = maximum lifespan – age at sexual maturity). Figure 4d shows that lifetime fertility is statistically invariant with adult body size across the lineages, consistent with Charnov et al. [25]. So, even though the allocations to the components of fertility differ conspicuously between the lineages in terms of litter size and frequency, the overall scaling of both annual fecundity and lifetime fertility is predictable though with limited precision from adult body size.

For all variables, values for monotremes tend to overlap those of similar-sized marsupials.

(c) Mass-specific production

Mass-specific production rate, calculated using equation (1.3), is very similar between marsupials and placentals. This is evidenced both by the extensive overlap in values for the two groups in figure 5 and by the parameters of the fitted regression models (table 2): marsupials \( \beta = -0.40 \pm 0.08 \) (95% CI) and placentals \( \beta = -0.37 \pm 0.02 \). A GLM testing for differences between the slopes and intercepts, while controlling for lineage and order, shows that the groups collapse onto a single scaling function, where \( \beta = -0.37 \pm 0.04 \). To control for the effects of phylogeny at a finer grained taxonomic level, we also ran a model that nested families within order, but the slopes and intercepts were not significantly different from the model controlling solely for order.

4. DISCUSSION AND CONCLUSIONS

Our data analysis not only quantifies well-known differences in life histories among the lineages but also offers new insights into the variation in life-history strategies within and among these groups. The differences in absolute values and allometric scalings of the various life-history traits among placentals, marsupials and monotremes reflect different ways that these three lineages have adapted to allocate time and energy to growth and development in order to maximize reproductive output. These differences reflect a complex combination of phylogenetic constraints owing to ancient divergence and selection owing to environmental conditions during subsequent evolution. Despite these differences in reproductive strategies, however, female placentals, marsupials and monotremes of the same body size all allocate energy to reproduction at essentially the same rate.

An important life-history parameter not considered in equation (1.3) is pre-weaning survival, which would adjust production values by accounting for offspring that received energy investment from the mother, but died before weaning [25]. However, accurate measures of pre-weaning survival are extremely rare, especially in wild populations. To estimate the effect of pre-weaning survival on mass-specific production, we used a method similar to Charnov et al. [25]. Using a small sample of placentals \((n = 13)\), Charnov et al. [25] show that pre-weaning survival rates scale with litter size as \( s_0 = 0.71^{-0.35} \) \((r^2 = 0.69, \ p < 0.01)\). We collected...
available data on marsupial pre-weaning survival ($n = 9$), and found that pre-weaning survival is approximately invariant with litter size as $s_w = 0.6^{0.03} \ (r^2 = 0.02, p > 0.05)$, but scales positively with body size, $s_w = 0.2 m^{0.1} \ (r^2 = 0.32, p < 0.05)$ (see appendix A for table of data and sources). The differences in the independent variables in offspring survival here probably follow from the differences in reproductive strategies between placentals and marsupials. For example, pouch-rearing in marsupials probably decreases litter size but increases pre-weaning survival as pre-weaned offspring effectively take on the mothers’ mortality, whereas in placentals, pre-weaned offspring are exposed to many additional sources of mortality, resulting in lower survival and so larger litter sizes. Therefore, we estimated pre-weaning survival rates from adult body size data for marsupials and from litter size data for placentals. For each species, we calculated the survival-corrected mass-specific production, $p \cdot s_w$ and plotted this as a function of log body size (figure 6). A GLM showed no significant difference between marsupial and placental production rates, and resulted in an overall scaling slope of $-0.33 \pm 0.07$, which is not significantly different from the uncorrected analyses. Thus, despite the different effects of pre-weaning survival on the ecologies of marsupials and placentals, its effect on production is consistent across lineages, reducing the overall scaling exponent slightly from between $-0.37$ and $-0.40$ to $-0.33$.

The relatively tight clustering of data about the regression lines in figures 5 and 6 is predicted by metabolic scaling theory on the grounds that all types of mammal are subject to essentially the same constraint on production rate. However, scaling theory would predict a slope of $-1/4$, whereas the observed slope is closer to $-1/3$. This discrepancy occurs because weaning mass is not a constant function of adult mass, but scales sublinearly with an exponent of $-0.87$ for marsupials and $-0.91$ for placentals (figure 5). Why does relative weaning mass scale negatively? We offer three hypotheses for future consideration: (i) Larger mammals differentially allocate resources to adult survivorship at the expense of weaning mass. This should be particularly advantageous in seasonal environments, where it helps adults to survive the winter. (ii) Seasonality should place additional demands on small mammals that breed more than once a year. By producing relatively large offspring, mothers increase the chance their offspring survive a stressful period. (iii) Capital breeding (i.e. fueling reproduction from stored reserves) is increasingly common in larger mammals. Fitness tradeoffs associated with acquisition, storage and mobilization of stored reserves may favour reducing size of offspring at weaning in larger mammals.

The interactions and replacements that occurred when the previously isolated lineages came into contact, such as occurred when the Panamanian land bridge allowed interchange between North and South America approximately 3 Ma ago or when modern humans introduced placental mammals into Australia, have often been attributed to

Figure 4. Bivariate log–log plots of components of fecundity as a function of adult body mass: (a) litter size, (b) litter frequency, (c) annual fecundity, and (d) lifetime fecundity.

Figure 5. Bivariate log–log plot of mass-specific production as a function of adult body mass. A GLM testing for differences in scaling among lineages finds no significant difference, and gives an overall slope of $-0.37$. See table 2 for further details.

Figure 6. Bivariate log–log plots of mass-specific production as a function of adult body mass. A GLM testing for differences in scaling among lineages finds no significant difference, and gives an overall slope of $-0.37$. See table 2 for further details.
power of body size (figure 4a,b), with the result that annual fecundity scales similarly across the lineages, and lifetime fertility is invariant (figure 4c,d).

The strikingly similar scaling of production in monotremes, marsupials and placentals suggests that the evolutionary pathways that led to the seemingly divergent mammalian physiologies, reproductive ecologies and life histories are metabolically equivalent ways of being a mammal.

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**APPENDIX A. MARSUPIAL PRE-WEANING SURVIVAL DATA**

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<tr>
<td>Macropus rufigrivasus</td>
<td>0.65</td>
</tr>
</tbody>
</table>

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