The measure and significance of Bateman’s principles

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Bateman’s principles explain sex roles and sexual dimorphism through sex-specific variance in mating success, reproductive success and their relationships within sexes (Bateman gradients). Empirical tests of these principles, however, have come under intense scrutiny. Here, we experimentally show that in replicate groups of red junglefowl, Gallus gallus, mating and reproductive successes were more variable in males than in females, resulting in a steeper male Bateman gradient, consistent with Bateman’s principles. However, we use novel quantitative techniques to reveal that current methods typically overestimate Bateman’s principles because they (i) infer mating success indirectly from offspring parentage, and thus miss matings that fail to result in fertilization, and (ii) measure Bateman gradients through the univariate regression of reproductive over mating success, without considering the substantial influence of other components of male reproductive success, namely female fecundity and paternity share. We also find a significant female Bateman gradient but show that this likely emerges as spurious consequences of male preference for fecund females, emphasizing the need for experimental approaches to establish the causal relationship between reproductive and mating success. While providing qualitative support for Bateman’s principles, our study demonstrates how current approaches can generate a misleading view of sex differences and roles.

1. Introduction

In a pioneering study published in 1948, Bateman [1] extrapolated from experimental results in Drosophila melanogaster to propose that intrasexual selection is normally more intense in males because typically (i) compared with females, males have higher variance in number of mates (i.e. mating success); (ii) males also have higher individual variation in the number of offspring produced (i.e. reproductive success) than females and (iii) the slope of the relationship between mating and reproductive success (Bateman gradient) is steeper in males than in females. These observations became known as Bateman’s principles [2,3]; their formalization through selection analysis [4,5] marked the advent of modern sexual selection theory [5–7]. Bateman’s principles provide a conceptual explanation for Darwin’s observations that sexual selection is typically more intense in males and that males are often ‘eager’ to mate whereas females are ‘coy’ [8]. This Darwin–Bateman paradigm represents the foundation of our understanding of the evolutionary ecology of sex-specific selection, sex roles and sexual dimorphism [3,9].

A number of empirical studies have provided qualitative support for Bateman’s principles and their link with sex roles [3,10–17]. Recent work, however, has highlighted a number of problems with both the measurement and interpretation of Bateman’s principles [18–21], calling into question the magnitude...
of the estimated sex differences and their eco-evolutionary significance for four main reasons. First, Bateman gradients are measured by inferring mating success from offspring parentage [5,19,22,23], based on the assumption that an individual sires offspring with each of its mates. However, this assumption is problematic especially when polyandry generates sperm competition, which can result in males gaining no paternity despite behaviourally successful matings. Inferring mating success from offspring parentage in the absence of independent data on mating behaviour can thus introduce a source of error in estimates of male Bateman gradients. In most studies, measures of mating success based on parentage also capture, implicitly or explicitly, components of offspring survival (e.g. [24], reviewed in reference [25]), which can further bias estimates of Bateman gradients [26,27]. However, the magnitude of this potential source of error remains untested. Moreover, because—all else being equal—the probability of a male fertilizing at least one egg is a function of clutch size, the bias introduced by inferring male mating success from parentage is expected to be inversely proportional to average clutch size [22]. A better alternative to inferring mating success from offspring parentage is to observe mating behaviour directly and record mating rates for each individual [14]. However, the use of mating rates often fails to distinguish between an individual mating multiple times with the same partner, or mating once with multiple partners [28]. This distinction is crucial, because remating with the same partner and mating with multiple partners may influence the reproductive success of an individual in drastically different ways. In males, for example, remating with the same female would influence a male’s chances of fertilizing her eggs, whereas mating with multiple females would directly contribute to his mating success. One would therefore need to measure the actual number of mates for each individual, controlling for the potentially confounding effect of number of matings obtained with each mate. This requires intensive observations of individually tagged males and females [17,29].

Second, measuring the Bateman gradient as the slope of the linear least-square regression of reproductive success over mating success may be simplistic, because even with unlimited availability of mating opportunities the reproductive success of an individual is, at some point, limited by intrinsic reproductive costs such as the production of enough gametes [30]. It is therefore plausible that variation in reproductive success may be better characterized as a positive quadratic function of mating success. This is important because it suggests that sex differences may occur not only in the slope of linear functions of reproductive success (mating success), but also in the shape of such functions. The comparison between the maximum of the curvilinear function with the average mating success of a population enables one to test whether the reproductive success of members of one sex in a population is limited by the availability of mating opportunities (maximum > average mating success) or by intrinsic reproductive costs (maximum < average mating success [30]).

Third, polyandry makes the relationship between mating and reproductive success more complex [9,31–33]. With polyandry, the reproductive success of an individual male is the product of his mating success, the fecundity of his mates (mate fecundity) and the proportion of ova fertilized within the clutch of each female he mated with (paternity share). Because Bateman gradients are measured as the slope of the univariate least-square regression of reproductive success over mating success, they capture both direct selection on mating success, but also indirect selection on other components of reproductive success if mating success covaries with mate fecundity and/or paternity share. Hence, the Bateman gradient behaves as a selection differential rather than act as a selection gradient as it encompasses direct and indirect selection on mating success [34]. For example, the male Bateman gradient can be inflated via paternity share if, for a given male fecundity, males that mate with more females have on average a higher paternity share of each clutch [35]. Alternatively, by mating with more females, males might suffer from reduced paternity share through trade-off mechanisms [36]. One way to measure the relationship between mating and reproductive success controlling for these covariances is to use a traditional multivariate approach such as

\[ \text{Reproductive success} = \beta X + \epsilon, \]

where \( \beta \) is the vector of partial regression coefficients on mating success, mate fecundity and paternity share, \( X \) the matrix of phenotypic values for those traits and \( \epsilon \) an error term of 0 mean [34].

Finally, it is becoming clear that females can also have positive Bateman gradients, even in species with typical ‘sex roles’ [18,37–39], which suggests that sexual selection for mating success might also be significant in females [2,18,40–43] potentially owing to cumulative benefits associated with mating [44,45]. Note that this is not necessarily inconsistent with the Darwin–Bateman paradigm provided that the Bateman gradient is steeper in males than in females in a given species. However, the significance of female Bateman gradients and the relative strength of sexual selection on female mating success remain debatable [22,45,46]. Alternatively, a positive female Bateman gradient may arise if more fecund females are exposed to higher mating rates solely because they are more attractive to males, thus reversing the causality of the relationship between female mating and reproductive successes [22,47,48]. Explicit tests of the significance of female Bateman gradients remain scarce.

Here, we combine an experimental approach with multivariate analyses to address these issues and resolve the significance of Bateman’s principles in replicate groups of red junglefowl, Gallus gallus. First, we test Bateman’s principles using the traditional approach of inferring mating success from genetic parentage of offspring (MSgen) and univariate regressions of reproductive success on mating success inferred from offspring parentage. Second, we measure mating success using fine-grained mating behaviour data to measure the bias introduced by the traditional use of mating success inferred from parentage. Third, we use a multivariate approach to quantify the relationship between male mating success and reproductive success, controlling for mate fecundity, paternity share and their covariances with mating success. Finally, we explore the causality of female Bateman gradients by testing whether variation in female mating success causes changes in female reproductive success.

### 2. Material and methods

(a) Observations and parentage assignment in semi-natural conditions

We studied a population of red junglefowl at the field station of the University of Oxford between May–September 2007 and
August–September 2008, as detailed in reference [35]. Briefly, we observed 13 replicate groups of three adult males and four adult females in outdoor pens, typical group size and sex ratio in natural groups [49]. In each replicate group, we monitored mating behaviour for 10 consecutive days. We collected all the eggs laid in each group from the second day of observation (i.e. the first day in which inseminations may have resulted in fertilization) and for the subsequent 10 days (i.e. day 2–11 inclusive, see the electronic supplementary material, table S1 on variation in female reproductive success). One group departed from this pattern as egg collection occurred from day 7 to day 16. We tested the effect of removing this group from the analysis, but as no qualitative difference was observed, we present only the results of the full dataset. We incubated eggs artificially for 7 days when we collected the embryos of fertilized eggs. In order to measure whether sperm depletion was likely to create sexual selection in females, we recorded the percentage of eggs that showed no evidence of embryo development (indicating that the eggs were either not fertilized or suffered embryo death within the first hours of development) in five of the 13 replicate groups. In these five groups, 11% of the eggs showed no sign of embryo development. More than half of these eggs were laid in the first days of egg collection, suggesting that they were not fertilized owing to the expected delay between insemination and fertilization [50]. Excluding eggs laid in the first 2 days, reduced the proportion of eggs with no sign of embryo development to 5%. Collectively, these results indicate that if some fertilizations went undetected in the study, then these represented a small proportion of the eggs. All embryos (n = 254) were genotyped at seven variable microsatellite loci [50], their paternity and maternity were successfully assigned in CERVUS 3.0 ([35,51,52] and the electronic supplementary material, table S2).

(b) General analytical approach

Reproductive success in males and females was calculated as the number of embryos produced by each individual. Mating success inferred from genetic parentage of the offspring (MSgen) was calculated as the total number of mates with whom an individual produced offspring. Importantly, we also measured ‘total’ male and female mating success (MSma) by adding to MSgen any additional mate with whom a focal individual had been observed successfully copulating during the 10 day period of observation but to which no offspring were assigned. To control for the potential effects of mating repeatedly with the same mate, we entered as a covariate the average number of successful matings that a focal individual was observed to have with each mate. As no difference was observed by adding this covariate, we did not report results of analyses that included it. In addition, for males, mate fecundity was calculated as the average number of eggs laid by all females with whom a male produced offspring, corrected by the number of eggs laid by all females with whom a male was observed to copulate successfully (see calculation of MSma above). Accordingly, the paternity share of a male was calculated as the proportion of embryos sired out of the total number of embryos produced by all the females with whom he successfully mated. We calculated the opportunity for total sexual selection (I from sensu [35]) as standardized variance in reproductive success [4,33,54]:

\[ I = \frac{\sigma^2}{\bar{t}^2}, \]

(2.1)

where \( \sigma^2 \) represents the variance in reproductive success, and \( \bar{t}^2 \) is the square mean of the reproductive success of members of one sex in a group. Similarly, we calculated the opportunity for sexual selection on mating success, \( I_s \) (from sensu [35]) as the standardized variance in mating success:

\[ I_s = \frac{\sigma^2}{MS} \]

where \( MS \) represents the mean of the variance in the number of offspring produced by each mate.

We also used a novel method described by Moorad & Wade [55] to determine the proportion of \( I \) explained by the different components of male sexual fitness in the univariate analysis, namely mating success, mate fecundity and paternity share. In brief, we partitioned \( I \) into additive components (either only \( I_s \) in the univariate analysis, or with the other components of male sexual fitness in the multivariate analysis), and significance was tested by normal bootstrapping [56] to estimate confidence intervals. Finally, to obtain results comparable with other organisms with various population and clutch sizes, we produced a standardized measure of Bateman gradients [2]. We standardized Bateman gradients as usually done for selection gradients by dividing reproductive success by the average population score (relative fitness), whereas each individual trait (mating success, mate fecundity and paternity share) was subtracted by its population mean and then divided by its standard deviation in the population, to obtain a mean of zero and a standard deviation of unity.

In the models comparing different ways of calculating the Bateman gradients, estimates of all gradients were deduced from a simple linear model of male or female reproductive success and different predictors [5]. To obtain the significance of fixed effects and overall fit of models, we performed generalized-mixed models (Imer, library lme4 in R v. 2.15.2, R Core Team [57]), with replicate group as random effect with 13 levels. Some birds were used in more than one replicate group (four males used in two groups, four in three groups, one in four groups, nine females in two groups and seven females in three groups). Repeatability in the components of reproductive success (total reproductive success, mating success, mate fecundity and paternity share) across groups was consistently low in males [35]. For males used in multiple groups within the same reproductive season, relative male’s reproductive performances in one group were poor predictors of their relative performance in the next group (reproductive success: adj. \( R^2 = 0.07 \); mating success: adj. \( R^2 = 0.07 \); mate fecundity: adj. \( R^2 = 0.08 \); paternity share: adj. \( R^2 = 0.08 \)). Similarly, the relative reproductive and mating success of a female in a group did not predict her reproductive success and mating success in the next replicate group within the same year (reproductive success: adj. \( R^2 = -0.01 \); mating success: adj. \( R^2 = -0.05 \)), suggesting that the reproductive performance of these birds was largely contingent on the dynamics of different replicate groups rather than consistently determined by inherent properties of the individual or by seasonal patterns. Nevertheless, bird identity nested within group was fitted as an observation-level random effect to control for pseudo-replication and overdispersion. In all mixed models, the response was male or female reproductive success which was fitted as a Poisson distribution; hence, we used a log link function to test the fixed effects. The significance of each fixed effect was tested by a log-likelihood ratio test comparing models fitted by the Laplace approximation including or excluding the tested fixed effect. However, because the log-likelihood ratio test is considered non-conservative for fixed effects [58], and because the log link function does not directly test the linear relationship that the Bateman gradient aims to describe, we calculated confidence intervals for each estimate of slope with bootstrapping methods. We first fitted a linear-mixed model (Ime, library nlme, in R v. 2.15.2) on reproductive success with the fixed effects. We then shuffled the residuals given by this model, added them to the fitted values and refitted the model to these newly created datasets [59]. To be conservative, we repeated this bootstrapping method 2000 times on mixed models including either (i) the bird identity, (ii) the group of birds and (iii) the bird identity nested within the group of birds as random effects. The results presented include 0.95 confidence intervals given by these simulations.

(i) The traditional measure of Bateman’s principles

We calculated the total opportunity for selection (I), and the opportunity for sexual selection (I_s) for males and females as the standardized variance in mating success inferred from
genetic parentage (MSgen). We also calculated confidence intervals on I indices and the percentage of I explained by I_{hA} [55]. Male and female Bateman gradients were calculated independently by using male and female MSgen as fixed effects in the models above. To compare male and female Bateman gradients, we merged male and female datasets and computed mixed models fitted with a Poisson distribution that used, without intercept (i) sex and MSgen as fixed effects and (ii) sex, MSgen and the interaction between both as fixed effects. The comparison between (i) and (ii) by a log-likelihood ratio test quantified the statistical significance of the difference between male and female Bateman gradients. We also tested for quadratic effects by adding MS_{gen}^{2} as a fixed effect and calculated confidence intervals for MS_{gen} and MS_{gen}^{2} as previously described.

(ii) The bias introduced by inferring mating success from offspring parentage
To investigate the effect of matings not resulting in fertilization on Bateman’s principles, we recalculated male and female I_s and Bateman gradients as above, using MS_{tot} instead of MS_{gen}. We then compared the general fit and the Akaike information criterion (AIC) of models based on MS_{gen} versus MS_{tot}.

(iii) The multivariate measure of Bateman’s principles
To test whether the opportunity for sexual selection (I_i) and the Bateman gradients were artificially inflated by the covariances of mating success with other components of male reproductive success [35], we added male mate fecundity and paternity share to the model. We first calculated opportunity of selection on mate fecundity and paternity share as described in reference [55]. Second, we tested the effect of adding mate fecundity and paternity share in the calculation of the Bateman gradient by comparing the goodness of fit and the AIC of the generalized-mixed models. We also tested the effect on male reproductive success of the covariances between all components of male reproductive success by adding second-degree interactions to the model, but as this was not significant we do not report it here.

(iv) The significance of female Bateman gradients
We explored the hypothesis that a positive female Bateman gradient arises because mating with additional males causes an increment in female fecundity (adaptive hypothesis). The adaptive hypothesis predicts a specific temporal pattern, whereby female reproductive rate (i.e. the probability to lay a fertile egg on a given day) increases over successive days for polyandrous females, as they accumulate additional partners, but remains constantly low in monandrous females. There are two alternative (null) hypotheses for a positive female Bateman gradient. First, inherently more fecund females mate with more males. Second, even if all females mate with the same number of males, then inherently more fecund females will, in principle, produce more eggs, have a higher probability of producing fertile offspring sired by more males. However, measuring mating success based on behavioural data should make this latter explanation less likely to apply to our study. Neither of these alternative scenarios predicts temporal changes in the reproductive rate of polyandrous versus monandrous females over the course of a trial. We therefore analysed variation in the probability that a female would lay a fertile egg on a given day over successive days of the trial in relation to her cumulative mating success (female MS_{tot} = 1, 2 or 3), with a mixed model fitting a binomial distribution and, including trial day, MS_{tot}, and day × MS_{tot} interaction as fixed effects.

We then conducted an experiment to test the causal relationship between female mating and reproductive successes. Monoandry and polyandry treatments were sequentially conducted in random order on 13 females. Females received controlled matings [60] in the afternoon on 3 consecutive days, either three times with the same male (monoandry) or with three different males (polyandry). Egg laying rate was monitored for each of the females for the 7 days following the treatment [50]. Females were housed in groups, and eggs were assigned to females using orally administered coloured lipid dyes [60]. We compared the number of eggs laid by a female following the polyandry treatment with that of the same female following the monoandry treatment, with a paired t-test. As our sample was rather limited (n = 13), we conducted a power analysis to estimate the likelihood of finding an effect size similar to the one observed in the semi-natural groups. We ran a model simulating a Poisson distribution with the same sample size and average number of eggs laid as in the controlled mating experiment. The power analysis showed that we had 79.2% chance of detecting the difference in fecundity between females mated to one and females mated to two males observed in the semi-natural groups. Note that this power analysis is conservative because it does not consider the within-female paired design.

3. Results

(a) The traditional measure of Bateman’s principles
The opportunity for selection was almost twice as high in males as in females (table 1). Similarly, the opportunity for sexual selection on mating success was approximately four times higher in males than in females, and was significantly positive in both sexes (table 1). The variance in mating success explained 56.9% of the variance in reproductive success in males, but only 24.1% in females (table 1). Finally, the male Bateman gradient was significantly steeper than the female gradient, as indicated by the comparison between a model, including the fixed effects sex and MS_{gen} and a model, including sex, MS_{gen} and the interaction between both (I^2 = 9.4, p = 0.002; figure 1a). However, the Bateman gradient was significantly positive in both males and females (figure 1a and table 1). Standardized measures of male and female gradients produced a qualitatively similar pattern (table 1). We detected a positive quadratic relationship between reproductive and mating successes in females (estimate MS_{gen} = 5.65 [3.60; 7.60], estimate MS_{gen}^{2} = −1.25 [−1.89; −0.65]; figure 2b) but not in males (estimate MS_{gen} = 1.84 [−0.65; 4.32], estimate MS_{gen}^{2} = 0.61 [−0.01; 1.23]). The female quadratic function was maximized when females had 2.26 partners (female MS_{gen} = 2.26 [CI 0.95; 6.04]), which was very close to the average female mating rate in the population (average MS_{gen} = 2.14, figure 1b). (b) The bias introduced by inferring mating success from offspring parentage
Overall, 29.4% of the pairs that were observed mating did not sire offspring together and were therefore missed by estimates of mating success based on genetic parentage assignment (i.e. male and female MS_{gen}). When taking into account matings that did not result in fertilization by correcting data on mating success based on parentage with behavioural observations (MS_{obs}), the opportunity for sexual selection on mating success dropped in males (male I_s = 0.34 [CI: 0.16; 0.53]) and became null in females (female I_s = 0.03 [CI: −0.06; 0.09]; table 1). Similarly, when correcting data on mating success based on parentage with behavioural observations, the variance in mating success explained 42.5% of the variance in male reproductive success and only 5.4%
of the variance in female reproductive success (table 1). Correcting data on mating success based on parentage with behavioural observations also greatly changed the models estimating male and female Bateman gradients (table 1). The Bateman gradient remained significantly positive in both males and females (table 1) after correcting data on mating success based on parentage with behavioural observations. However, both male and female gradients were reduced, indicating that the traditional use of mating success based on parentage can lead to considerable errors in the estimates of both unstandardized and standardized Bateman gradients for males and females (table 1).

Converting data on mating success based on parentage with behavioural observations also greatly changed the models estimating male and female Bateman gradients (table 1). The Bateman gradients estimated using standard methods and standardized following [2]. The overestimation of the Bateman gradient calculates how much the Bateman gradient, measured using the traditional univariate approach, overestimates the relationship between reproductive and mating success. We obtained p values and AIC through a generalized-mixed model fitted with a Poisson distribution (see methods).

### Table 1.

<table>
<thead>
<tr>
<th>Model</th>
<th>Sex</th>
<th>Parameter</th>
<th>$i$ [%] (95% CI)</th>
<th>$i$ (% of I)</th>
<th>fit of the model [% of I]</th>
<th>Gradient [CI]</th>
<th>Gradient (standardized)</th>
<th>AIC</th>
<th>Overestimation of the Bateman gradient (%)</th>
<th>Overestimation on standardized data (%)</th>
<th>p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Traditional</td>
<td>Male</td>
<td>Mating success</td>
<td>0.46 [0.27; 0.65]</td>
<td>56.9</td>
<td>56.9</td>
<td>4.23 [3.66; 5.21]</td>
<td>0.81</td>
<td>59.9</td>
<td>&lt; 0.001</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Female</td>
<td>Mating success</td>
<td>0.11 [0.00; 0.22]</td>
<td>24.1</td>
<td>24.1</td>
<td>1.87 [1.15; 2.59]</td>
<td>0.34</td>
<td>103.6</td>
<td>&lt; 0.001</td>
<td></td>
<td></td>
</tr>
<tr>
<td>MS$_{tot}$</td>
<td>Male</td>
<td>Mating success</td>
<td>0.34 [0.16; 0.53]</td>
<td>42.5</td>
<td>42.5</td>
<td>2.82 [1.73; 3.92]</td>
<td>0.60</td>
<td>81.6</td>
<td>50</td>
<td>35</td>
<td>&lt; 0.001</td>
</tr>
<tr>
<td></td>
<td>Female</td>
<td>Mating success</td>
<td>0.03 [−0.06; 0.09]</td>
<td>5.4</td>
<td>5.4</td>
<td>1.50 [0.44; 2.45]</td>
<td>0.24</td>
<td>116.8</td>
<td>25</td>
<td>42</td>
<td>0.001</td>
</tr>
<tr>
<td>Multivariate</td>
<td>Male</td>
<td>Mating success</td>
<td>0.22 [0.08; 0.37]</td>
<td>27.8</td>
<td>96.3</td>
<td>1.67 [0.72; 2.62]</td>
<td>0.35</td>
<td>22.5</td>
<td>153</td>
<td>131</td>
<td>&lt; 0.001</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Female fecundity</td>
<td>0.00 [−0.02; 0.02]</td>
<td>0.0</td>
<td></td>
<td>1.79 [1.33; 2.25]</td>
<td>0.42</td>
<td>116.8</td>
<td>25</td>
<td>42</td>
<td>0.001</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Paternity share</td>
<td>0.55 [0.32; 0.80]</td>
<td>68.5</td>
<td></td>
<td>16.77 [13.70; 19.71]</td>
<td>0.70</td>
<td></td>
<td></td>
<td></td>
<td>&lt; 0.001</td>
</tr>
</tbody>
</table>

Figure 1. (a) Male (solid squares and line) and female (empty diamonds, dashed line) Bateman gradients based on MS$_{gen}$. (b) The quadratic relationship between female MS$_{gen}$ and reproductive success over a MS$_{gen}$ range of 0 – 3. Vertical bars represent 95% CI. The function shows a maximum for MS$_{gen}$ = 2. The vertical dashed line shows (approximately) mean female MS$_{gen}$ across groups. The dotted line around the line represents 2 SE around the mean.

The vertical dashed line shows (approximately) mean female MS$_{gen}$ across groups. The dotted line around the line represents 2 SE around the mean.
success, the traditional univariate approach overestimated the opportunity for covariances between these components of male reproductive paternity share (table 1), and revealed that, by failing to control for covariances between mating success (i.e. Bateman gradient), mate fecundity and paternity share in a multivariate framework that takes into account the covariances between male components of reproductive success explained more than 96% of the opportunity for selection in males (I), resulting in a significant improvement on the explanatory power of male reproductive success and in a lower AIC than that of the univariate model based on MStot (table 1). This multivariate model identified three independent sources of selection on male reproductive success: mating success (i.e. Bateman gradient), mate fecundity and paternity share (table 1), and revealed that, by failing to control for covariances between these components of male reproductive success, the traditional univariate approach overestimated the male Bateman gradient by more than 153% of the unbiased selection gradient (table 1). Again, the use of standardized gradients qualitatively agreed with this result (table 1).

(c) The multivariate measure of Bateman’s principles
Taking into account the covariances between male components of reproductive success explained more than 96% of the opportunity for selection in males (I), resulting in a significant improvement on the explanatory power of male reproductive success and in a lower AIC than that of the univariate model based on MStot (table 1). This multivariate model identified three independent sources of selection on male reproductive success: mating success (i.e. Bateman gradient), mate fecundity and paternity share (table 1), and revealed that, by failing to control for covariances between these components of male reproductive success, the traditional univariate approach overestimated the male Bateman gradient by more than 153% of the unbiased selection gradient (table 1). Again, the use of standardized gradients qualitatively agreed with this result (table 1).

(d) The significance of female Bateman gradients
Contrary to the predictions of the adaptive hypothesis and consistent with those of the null hypotheses, we found that the probability of laying an egg did not change with time (i.e. throughout the duration of a trial), but was consistently higher for females with higher mating success (MStot: $\chi^2 = 6.79, p = 0.01$, day: $\chi^2 = 0.02$, $p = 0.88$, day $\times$ MStot: $\chi^2 = 0.080$, $p = 0.78$).

In the controlled mating experiment, females did not produce more eggs when they were mated to different males (polyandry) than when they were repeatedly mated to the same male (monoandry, $t = -0.41$, d.f. = 12, $p = 0.69$; figure 2).

4. Discussion
Bateman’s principles are a cornerstone of modern sexual selection theory, yet intense recent debate has called into question their measure and relevance in studying sex differences [18,21,61–64]. Our study contributes to this ongoing debate by demonstrating that the traditional use of MSgen can generate severely misleading estimates of Bateman’s principles. Because matings can fail to result in fertilization, particularly in polyandrous species, the number of females with whom a male mates successfully can only be as great as the number of females with whom he sires offspring and typically lower than this (i.e. MStot $\geq$ MSgen). This inequality means that inferring mating success from offspring paternity is likely to introduce a systematic bias, by overestimating the opportunity of sexual selection on males. Importantly, for a constant share in paternity and mate fecundity, the total reproductive success of a male is directly proportional to his mating success inferred from offspring paternity but is independent from residual mating success that fails to result in paternity. Failing to consider this latter component of mating success is therefore likely to overestimate the steepness of the male Bateman gradient [17], and, because the probability of fertilizing at least one egg increases with clutch size, this bias is likely greater in species with smaller clutches.

Another large source of error arises from the covariance of male mating success with the other constituents of male reproductive success, namely mate fecundity and paternity share, which are not considered in the traditional univariate approach to Bateman’s principles. In red junglefowl, male mating success and paternity share may covary for different reasons. In our study population, males with high mating success also tend to enjoy high paternity share. This appears to be mediated by social dominance which allows a male to access more females and repeated mating opportunity with each female, which conveys a sperm competition advantage (high paternity share), likely through a replenishment of the male’s sperm in the female’s sperm storage tubules [35]. An alternative scenario may arise when males invest in either mating opportunities or fertilization efficiency through alternative mating tactics [65]. Under such conditions, males with high mating success may be poor sperm competitors and suffer low paternity share, whereas males with high paternity share may suffer low mating success, resulting in negative (rather than positive) covariance between mating success and paternity share. Several studies have shown that in domestic fowl, socially dominant males tend to produce ejaculates of lower sperm swimming velocity than the ejaculates produced by their subordinates [66–68]. Controlling for mating frequency and number of sperm inseminated, higher sperm velocity would give subordinate males an advantage in sperm competition [69]. A negative covariance of mating success and paternity share may also be more likely to occur in species where repeated matings are less relevant, such as for example external fertilizers. Covariance between male mating success and mate fecundity may also introduce significant bias, if for example males with high mating success mated preferentially with more fecund females.

Measuring Bateman gradients taking into account male paternity share and mate fecundity is non-trivial and to the best of our knowledge, few studies have attempted this in the past. Fritzschke & Arnqvist [39] have used the covariance between a trait and the residual reproductive success unexplained by the Bateman gradient to measure the overall selection on mate fecundity and paternity share. This approach, however, is simplistic: the potential covariances between mating success and other components of male sexual fitness make reality more complex. We really need to integrate mating success, mate fecundity and paternity share in a multivariate framework that takes into account their covariances in order to accurately quantify sexual selection on mating success (i.e. the Bateman gradient), mate fecundity and paternity share. Few studies have attempted...
to quantify such covariances. A recent study of the hermaphroditic snail, *Physa acuta*, found significant covariances between different components of male reproductive success [28]. Similarly, studies of passerine birds forming social pair bonds have quantified the covariance between within- and extra-pair components of male reproductive success, demonstrating that such covariance can represent a substantial source of variation in male reproductive success in some populations [70,71], but less so in others [48,72]. In part, differences between these studies are likely to reflect a combination of biological factors, such as population size, patterns of variation in polyandry, mate availability and clutch size, and future studies should seek to resolve how Bateman principles can be modulated by these factors. Some discrepancies may also reflect methodological differences. For example, Pélissié et al. [28] attributed variance in remating rates with the same female to sexual selection on male mating success [28], although in red junglefowl mating repeatedly with the same female has been shown to have a direct influence on paternity share [35]. Similarly, the distinction between within- and extra-pair reproductive success is not readily applicable to species that lack social pair bonds.

Our results also confirm the concerns expressed by previous studies over the interpretation of female Bateman gradients [47,48]. Positive female Bateman gradients, while significantly lower than corresponding male Bateman gradients, have been shown in a number of species, for example, bank voles [15], wild turkey [16] and *Drosophila* [14,18]. However, the causality of the relationship between female mating and reproductive successes is often unclear. Using a traditional approach, one would be led to conclude that red junglefowl females are selected to mate with multiple males, and optimize mating success at around two males. Because this value does not differ significantly from the average female mating success observed in these groups, one would also be led to conclude that females are in control of mating rates [30]. However, these conclusions are misleading. Such a positive female Bateman gradient is likely to arise as a spurious consequence of more fecund females mating with more males, rather than as an adaptive consequence of female polyandry. That the adaptive hypothesis is unlikely to explain our observation of a positive female Bateman gradient is indicated by (i) the lack of a time lag, which would be required for polyandry to cause an increase in female fecundity, and (ii) the lack of any evidence that mating with additional males causes an increase in fecundity in the pair-wise controlled experiment. The null hypothesis, that females that are inherently more fecund attract more mates, is entirely consistent with our results and also more plausible given the biology of the study species. This pattern may arise through both female- and male-driven mechanisms. Female fowl tend to display a higher propensity to mate in periods when they ovulate than in periods when they do not, and males have been shown to preferentially target ovulating females [73], indicating that females that lay more eggs are likely to be more sexually promiscuous. Kokko et al. [62] emphasize the importance of establishing causality to understand Bateman’s principles. Our study indicates that this is particularly important when it comes to the interpretation of female Bateman’s gradients.

Clearly, the approach that we adopted to measure male reproductive success also suffers from its own limitations. First, we may have missed a proportion of matings. Although we monitored the populations throughout the daily peaks in mating activity (early morning and late afternoon [74]), it is certainly possible that some mating activity went unnoticed. If these matings resulted in fertilization, then they would have been accounted for by our measure of mating success which complements behavioural data with cases in which paternity data identifies mating events undetected by behavioural observations. In actual fact, such cases were rare in our study (7.3% of the total number of mates was missed by behavioural data and detected through offspring parentage assignment). This does not eliminate the possibility that we may have missed mating events that failed to result in fertilization. However, undetected matings that failed to result in fertilization would mean that the discrepancy between MSgen and MSsex is even greater than reported by our study, and thus the bias introduced by inferring mating success exclusively from offspring parentage is consequently also even greater than our study estimates. Second, the use of behavioural data requires some careful consideration and may need to be tailored to the specifics of different study organisms. In our study, we considered only sexually mature males and females during their breeding season, and counted only mating events that comprised the entire succession of behavioural steps concluding with a successful cloacal contact [35]. A more careful approach may be required by studies of natural populations with limited possibilities for experimental control, less complete information on the reproductive status of different individuals or where matings observed represent a non-random subset of the mating occurring in the population [75]. In addition, although we incubated eggs artificially and sampled embryos early in their incubation (on day 7 of 21 day incubation period), we cannot entirely rule out the risk that our measure of reproductive success may have been influenced by embryo mortality at very early stage of development (i.e. within the first approx. 24 h from fertilization), which may be difficult to detect without molecular assays. However, the proportion of eggs that was deemed infertile in our study represented approximately 5% of all the eggs collected. Therefore, if it occurred, undetected early embryo mortality would appear to have had only a modest contribution.

Finally, our study shows that while efforts to reduce error can generate estimates of Bateman’s principles that are quantitatively drastically different from estimates derived from traditional approaches, the patterns of sex-specific differences observed are qualitatively entirely consistent with the three Bateman’s principles. Namely, we found higher $I_1$ and $I_2$ in males than in females and stronger sexual selection on male rather than on female mating success. Therefore, while our study suggests that previous estimates of Bateman’s principles are likely biased, it also provides a robust confirmation that these principles are real and not entirely artefacts of methodological limitations. In conclusion, our experiment confirms the validity of Bateman’s principles in a semi-natural population, but simultaneously reveals the necessity to rethink traditional approaches to study the evolutionary ecology of sex roles.

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