Visual extrapolation under risk: human observers estimate and compensate for exogenous uncertainty

Paul A. Warren1,*, Erich W. Graf2, Rebecca A. Champion1 and Laurence T. Maloney3

1School of Psychological Sciences, University of Manchester, Manchester M13 9PL, UK
2School of Psychology, University of Southampton, Southampton SO17 1BJ, UK
3Department of Psychology, Center for Neural Science, New York University, New York, NY 10003, USA

Humans commonly face choices between multiple options with uncertain outcomes. Such situations occur in many contexts, from purely financial decisions (which shares should I buy?) to perceptuo-motor decisions between different actions (where should I aim my shot at goal?). Regardless of context, successful decision-making requires that the uncertainty at the heart of the decision-making problem is taken into account. Here, we ask whether humans can recover an estimate of exogenous uncertainty and then use it to make good decisions. Observers viewed a small dot that moved erratically until it disappeared behind an occluder. We varied the size of the occluder and the unpredictability of the dot’s path. The observer attempted to capture the dot as it emerged from behind the occluded region by setting the location and extent of a ‘catcher’ along the edge of the occluder. The reward for successfully catching the dot was reduced as the size of the catcher increased. We compared human performance with that of an agent maximizing expected gain and found that observers consistently selected catcher size close to this theoretical solution. These results suggest that humans are finely tuned to exogenous uncertainty information and can exploit it to guide action.

Keywords: exogenous uncertainty; maximum expected gain; cue combination; statistical approaches; motion extrapolation; decision under risk

1. INTRODUCTION

In crossing a busy road, the prudent pedestrian attempts to predict the future positions of cars and other vehicles, and plans a path to avoid them. In the laboratory, human ability to extrapolate the path of objects in motion is impressive over a variety of conditions; observers can accurately track objects through visual noise [1,2] or after a period of occlusion [3]. Motion extrapolation can occur with or without tracking eye movements [4]; when imagining a target [5]; or while expecting a target to reappear after occlusion [6,7]. During occlusion, smooth pursuit continues, albeit with reduced gain and eye velocity [7].

The pedestrian’s decision whether to act on the plan, though, should also reflect the uncertainty in extrapolation and, ultimately, the probability that this plan will lead the pedestrian safely to the other side of the street. If it is dark or rainy, then a decision not to cross might be best precisely because of increased uncertainty in the prediction.

In the last decade, researchers in the field of human perception and action have begun to investigate decision tasks where perceptual and motor uncertainty play critical roles. In these tasks, observers plan a movement, execute it and receive monetary rewards or penalties determined by the outcome of the movement (for review, see [8,9]). The outcomes ranged from hitting a target on a computer monitor [10–12], arriving at a goal in a specified time window [13], trading off speed and accuracy [14] or speed and information [15], or planning a series of movements [16,17]. Observers could maximize their expected gain (EG) only if they compensated for their own visual and motor uncertainty in planning movements. Participants in these movement-planning tasks typically (but not always) planned movements that came close to maximizing their EG. In doing so, they demonstrated that they—like the prudent pedestrian—take into account uncertainty in planning movement (in this case, their own motor and visual uncertainty).

In most of the studies just mentioned, the participants’ endogenous visual and motor ‘noise’ was the dominant source of uncertainty. The pedestrian, though, confronts an additional, exogenous uncertainty. The future locations of vehicles on roads are effectively stochastic because drivers can change direction and velocity in unpredictable ways.

In this article, we use a gambling task to investigate human ability to extrapolate the paths of objects engaged in a ‘random walk’, the future paths of which are only partly predictable. Observers can succeed in maximizing EG only if they correctly model the uncertainty intrinsic to the movement of the object whose path is extrapolated. We test whether human observers can model exogenous uncertainty and whether they can use this information to make good decisions.
Figure 1. Task and notation. (a) The participant first viewed a small dot that moved outward from the centre of a circular arena along a stochastic trajectory until it disappeared under an occluder (grey ring) with inner radius \( r_O \) and width \( W_O \). Two examples of trajectories (\( T_1 \) and \( T_2 \)) are shown. Only the moving dot was visible to the observer, not the static trajectory as drawn here. After the dot reached the occluder, it stopped, marking the point of occlusion (\( \theta_O, \theta_S \)) in polar coordinates. The dot remained visible for the remainder of the trial. (b) The observer then set the location (\( \theta_L \)) and width (\( \theta_C \)) of a circular segment (a ‘catcher’) intended to ‘capture’ the dot as it re-emerged from behind the occluder. Two examples of catchers are shown. If the dot reappeared within the circular segment marked by the catcher, then the participant earned a reward (gain) \( G \) and otherwise received nothing. (c) The probability of capture, \( p(\theta_L, \theta_C) \), depends on both the location \( \theta_L \) and width \( \theta_C \) of the observer’s setting of the catcher. We plot an example of \( p(\theta_L, \theta_C) \) as a function of \( \theta_C \) for the special case \( \theta_C = \theta_S \) (the observer has centred the catcher on the point of occlusion \( \theta_S \)). The probability of capture \( p(\theta_L, \theta_C) \) increases with capture angle \( \theta_C \) (dashed line). In the experiment, the magnitude of the reward \( G \) was determined by the experimenter and it decreased with the width \( \theta_C \) of the catcher. An example of \( G(\theta_C) \) versus \( \theta_C \) is plotted as a dash-dotted line. \( E(\theta_L, \theta_C) = p(\theta_L, \theta_C)G(\theta_C) \) is plotted versus \( \theta_C \) (solid line). The choice of catcher width \( \theta_C \), maximizing the observer’s \( E \) (for the choice of \( \theta_L = \theta_O \) used throughout this example) is marked with a dotted vertical line. In general, \( E \) depended on both the observer’s settings of the location \( \theta_L \) and capture angle \( \theta_C \) of the catcher.

The key aspects of the extrapolation task used in the present study are shown in figure 1. This approach has similarities to that used by Graf et al. [18]; however, in the present study, we incorporate a new risky decision-making task. Participants observe a circular arena and a small dot travelling on an irregular and unpredictable path outward from a central starting point (two such possible trajectories, \( T_1 \) and \( T_2 \), are shown in figure 1a, with \( T_2 \) less irregular than \( T_1 \)). The dot disappears when it hits the occluder at point \( (r_O, \theta_O) \) and the observer must adjust a circular segment (the ‘catcher’) to attempt to ‘capture’ the dot when it reappears on the outside on the occlusion region (figure 1b).

The observer is free to adjust both the location \( \theta_L \) of the centre of the catcher around the perimeter of the occluder and the angular extent \( \theta_C \) of the catcher \( \theta_C \). Once the observer has completed the setting, the point where the dot re-emerges is shown. If the dot re-emerges within the span of the catcher, the observer receives a monetary reward; otherwise, no reward is received.

The probability that the adjusted catcher will capture the dot, \( p(\theta_L, \theta_C) \), is an increasing function of \( \theta_C \) because for any fixed choice of \( \theta_L \), the probability of catching the dot cannot decrease as the angular extent of the catcher is increased. To illustrate this point, in figure 1c, we plot \( p(\theta_L, \theta_C) \) versus \( \theta_C \) (dashed line) for the special case where \( \theta_L = \theta_S \), that is, the observer has centred the catcher on the angular coordinate where the dot disappeared beneath the occluder. The function is increasing: the greater the angular extent of the catcher, the greater the chances the dot will be caught.

An observer wishing to simply capture the dot would set the catcher to its maximum width. However, in our experiment, the gain received for a successful capture depends on the observer’s choice of capture angle \( \theta_C \): the smaller the width of the catcher, the greater the reward (gain), \( G(\theta_C) \). We plot \( G(\theta_C) \) versus \( \theta_C \) in figure 1c (dash-dotted line) for one of the conditions of our experiment.

The \( E \) for any setting of the catcher (\( \theta_L, \theta_C \)) is then

\[
E(\theta_L, \theta_C) = p(\theta_L, \theta_C)G(\theta_C).
\]

(1.1)

plotted in figure 1c for the special case \( \theta_L = \theta_O \) (solid line).

As \( \theta_C \) changes, there is an evident trade-off between the probability of getting a reward and the amount of reward obtained. We verified computationally that there is a unique point (\( \theta_M^{\text{MEG}} \), \( \theta_C^{\text{MEG}} \)) that maximizes \( E \) in each of our experimental conditions. This setting \( \theta_C^{\text{MEG}} \), for the hypothetical case where the observer centres the catcher on the point of occlusion \( (\theta_S - \theta_O) \), is marked with a vertical dotted line in figure 1c. We compare human performance with ideal performance maximizing \( E \). We postpone discussion of how to compute the maximum expected gain (MEG) solution until after we describe the algorithm used to generate the stimuli in §2a.

2. EXPERIMENT

(a) Methods

(i) Observers

All observers were students or staff at Cardiff University and all took part in the experiment under informed consent. There were five observers, none of whom was aware of the hypotheses under test.

(ii) Apparatus

Stimuli were presented on a 22-inch flat-screen Viewsonic p225f CRT display (1024 x 768 pixels; 40 x 30”). Observers sat approximately 57.3 cm from the monitor.
and viewed the display binocularly. The centre of the screen was approximately at eye level.

(iii) Task
The task is schematically presented in figure 2. Observers watched a dot travel towards the inner edge of the occluder, at which point it stopped (figure 2a; note that the motion trail is presented for illustration purposes only and was not given in the experiment). Observers were then asked to try to ‘catch’ the dot when it emerged outside the occluder using an arc segment whose position and angular extent (the capture angle) could be varied—the ‘catcher’ described above (figure 2a). As the capture angle varied, so did the number of points that the observer could score if they caught the dot and the points. The points that could be won were presented adjacent to the catcher (figure 2b) and varied as the observer varied the width of the catcher.

The points scored if the dot was caught varied as a linear function of angular arc length from a minimum of 0.05 points when the arc length was 120° to a maximum of six points when the arc length was 180° (figure 1c, dash-dotted line). The maximum possible arc length was constrained to be 120°, and in practice observers never set the arc length to be this large.

Observers took on the order of 1–2 s to set the arc length. After the observer completed the setting, the position of the dot when it exited from behind the outer edge of the occluder was shown. If the final position of the dot on the outer edge of the occluder fell within the catcher set by the observer, then the catcher turned green, the observer was informed that they had caught the dot (HIT) and the associated points were awarded (figure 2b). If it did not, the catcher turned red, the observer was informed they had missed the dot (MISS) and no points were awarded (figure 2c).

(iv) Instructions
Observers were simply instructed to score as many points as possible during the experiment by catching the dot. We measured the observers’ settings of $\theta_L$ and $\theta_C$ on each trial. We attempted to increase observers’ motivation by awarding a bonus prize for the observer who scored the most points.

(v) Stimuli
The visual stimulus consisted of a single red dot moving on a random walk trajectory from the centre of the screen towards the inner edge of a grey annulus occluder on an otherwise blank screen (figure 1a). The distance from the start point to the inner edge of the occluder was $\alpha_0 = 6.5°$. On a given trial, the dot moved at a constant speed $s$ in a direction that changed at discrete
temporal intervals synchronized with the frame rate of the CRT (100 Hz).

(vi) The von Mises random walk
The changes in direction were random variables drawn from a von Mises distribution [19] with mean $0^\circ$ (‘straight ahead’). The variability of the random walk was controlled by a parameter $\kappa$. We refer to $\kappa$ as the directional reliability of the motion path. Trials with low values of $\kappa$ typically had more erratic paths than trials with high values. Figure 2d shows examples of paths that might be obtained when sampling from distributions with the values of $\kappa$ that we used in the experiment (for more details on the random walk process, see the electronic supplementary material).

When the dot reached the edge of the arena, we stopped the updating process and allowed the observer to set the catcher as described earlier. The observer was then shown the point at which the dot re-emerged from behind the occluder as determined by continuing the updating process. Note that, while unlikely, it was possible that the dot would pass back and forth from the occluder region to the central arena one or more times before finally emerging on the outer side of the occluder. The observer received a reward only if the dot first reached the outer edge of the occluder within the time limit set by the observer. Note the distance between the inner edge of the occluder and the centre of the arena is fixed in all trials. The state vector of the dot when it reaches the edge of the occluder is $(x_O, y_O, v_O)$, where $x_O$ and $y_O$ represent the dot position, and $v_O$ the instantaneous dot direction at occlusion. We may then represent the coordinates $(x_O, y_O)$ in polar coordinates as $(r_O, \theta_O)$, as shown in figure 1a. Then, because $r_O$ is a constant, the distribution of future paths of the point under the occluder is determined by $(\theta_O, v_O)$.

(vii) Design
The independent variables were the $\kappa$ parameter (50, 100, 200 and 600) illustrated in figure 2d; the occluder width, $W_O$ (1, 2.5, 4 cm); and the speed of the dot, $s$ (1.5, 3.0 deg s$^{-1}$). They were combined in a full factorial repeated-measures design to give 24 conditions. Observers undertook six repetitions of each of the 24 conditions in randomized order.

(viii) Dependent measures
We measured the position $(\theta_L)$ and capture angle $(\theta_C)$ of the capture region on each trial.

(ix) Statistical analysis
All capture angles are limited to between 0° and 120°. Because there is no danger of wrap-around, we report linear (rather than circular) descriptive statistics and conduct linear statistical analyses.

3. RESULTS

(a) Initial analysis
We conducted a preliminary three-factor repeated-measures ANOVA on the data. In a previous study, we had found no effect of speed and thus were able to collapse across this condition. In the present study, we found a similar pattern of results at the group level ($F_{1,4} = 0.874$, $p > 0.05$), and at the level of the individual observer (all $p > 0.05$ after Bonferroni correction; see electronic supplementary material). Therefore, our subsequent analyses have been conducted on the data collapsed across speed with effectively 12 distinct experimental conditions (4 directional reliabilities; $\kappa \times 3$ occluder widths, $W_O$).

(b) Point estimate data
The observer’s choice of $\theta_L$, the location of the capture region, can be treated as a point estimate of where the dot will emerge from behind the occluder. We will not focus on this aspect of the data in detail. Observers tend to centre the catcher at the angle $\theta_C$, at which the dot hit the inner edge of the occluder.

In figure 3, we plot histograms of the deviations $\theta_L - \theta_O$ of each setting from $\theta_O$ for each of the 12 conditions. As can be seen, in all conditions, the data are well described by a Gaussian distribution centred on 0 and with the same standard deviation as the data in the corresponding condition. The fitted distributions have relatively small standard deviations (the largest is approx. $17^\circ$).

This pattern may be expected given the information available to observers when setting $\theta_C$: they could see both the centre point of the arena, and the position of the dot as it hit the inner edge of the occluder. The observed data could result from a strategy of extending an imaginary line from the centre of the arena, through the point at which the dot entered the occluder to the outer occluder edge. Such a strategy would appear to not use information that might be obtained from the dot direction at the point where it hit the occluder; we will test for evidence of this in §3c.

(c) Prediction of catcher location settings
The distribution of future paths of the dot is determined by the state vector $(\theta_O, v_O)$ specifying where the dot reached the occluder and its instantaneous direction when it did so. Thus, if the dot was ‘turning’ clockwise or anti-clockwise as it reached the occluder, then it is possible that an observer might compensate by adjusting the location of the catcher clockwise or anti-clockwise.

In effect, would a regression model with both $\theta_O$ and $v_O$ better predict $\theta_L$ than $\theta_O$ by itself? To test for this possibility, we performed a linear regression analysis of setting $\theta_L$ on the independent variables $\theta_O$ and $\Delta v_O = v_O - \theta_O$. The latter independent variable is the deviation of $v_O$ away from $\theta_O$. We found no significant effect of $\Delta v_O$ on setting $\theta_L$ ($t_{507} = -1.219; p = 0.224$), but a highly significant effect of $\theta_O$ on setting $\theta_L$ ($t_{507} = 170.701; p < 0.0001$). The intercept term was not significantly different from 0 ($t_{507} = -0.710; p = 0.478$); that is, observers’ settings were not biased away from $\theta_O$. The overall $r^2 = 0.989$ was high. The same regression analysis was also performed on each observer’s data independently, with the same pattern of results for all observers (details given in the electronic supplementary material).

These outcomes are consistent with the claim that $v_O$ did not affect observers’ settings. Accordingly, we assume that observers set the location of the catcher $\theta_L$ to match $\theta_O$ and did not make use of an estimate of $v_O$, the direction the point was travelling when it reached the occluder. This outcome is perhaps not surprising because $\theta_O$ was marked with a visible red dot that remained on the screen during the setting, whereas $v_O$ (the direction of the last segment of the random walk) was difficult to estimate from the available visual
To address this question, we used Monte Carlo methods. For each of the 12 conditions of the experiment, we simulated 100 trajectories up to the occluder and, for each of these, calculated a further 1000 trajectories under the occluder (i.e. 100 000 trajectories in total per condition). For each of the 100 up to occluder trajectories, we calculated the circular standard deviation, \( \sigma_{\text{ext}}(\kappa, W_O) \), \( i = 1, 2, \ldots, 100 \) of the exit distribution over the 1000 under occluder trajectories [20]. We then took the circular average of the \( \sigma_{\text{ext}}(\kappa, W_O) \) over the 100 up to occluder trajectories. This resulted in a single trajectory variability estimate, \( \hat{\sigma}_{\text{ext}}(\kappa, W_O) \), for each of the experimental conditions. This approach is similar to that used by Graf et al. [18]. In doing so, we averaged out the effect of differences in the direction of the dot when it hit the occluder, \( \nu_O \), on the subsequent setting (because each of the 100 up to occluder trajectories would have a different \( \nu_O \)). However, as discussed earlier, this parameter has little additional influence on the setting beyond that of the position \( \theta_O \) at which the dot hits the occluder. Nonetheless, we maintain this approach because it ensures that the trajectories simulated and the subsequent calculations of \( \hat{\sigma}_{\text{ext}}(\kappa, W_O) \) take into account the possible variability in \( \nu_O \).

We reasoned that if observers could recover the variability in the trajectory, then their settings should be tightly correlated with the \( \hat{\sigma}_{\text{ext}}(\kappa, W_O) \) values obtained from the simulations. We fitted the data to a model

\[
\theta_{\text{C}} = \alpha(\sigma_{\text{ext}})^\beta W_O^\gamma
\]  

(3.1)

which includes a term \( W_O \). The actual fits were performed by a linear regression on the variables transformed by a natural logarithm

\[
\log \theta_{\text{C}} = \log \alpha + \beta \log \sigma_{\text{ext}} + \gamma \log W_O.
\]  

(3.2)

The results of the regression are presented in figure 4b. We find a strong relationship (\( r^2 = 0.915 \)) between \( \sigma_{\text{ext}} \)}
and observed capture angle with regressed capture angle averaged across observers given by:

\[ \theta_C = 75.79(\sigma^\text{ex})^{0.084} W_0^{0.225}. \]  

(3.3)

The regressed capture angles are superimposed on the plot of observed capture angle versus von Mises parameter \( \kappa \) in figure 4a (lines) and the regression is reported in figure 4b.

The resulting fit is close to the data except at the smallest value of \( \kappa \), suggesting that equation (3.1) is only approximate. In the electronic supplementary material, we report further analyses of these data, which suggest that the correct functional form for equation (3.1) is closer to a straight line than a power transformation over the range of \( W_0 \) employed in the actual experiment.

We conclude that the quantity that observers are encoding and reporting when making a capture angle setting is tightly coupled to a quantity reflecting the objective variability in the path directly. The next question to address is whether observers can use this variability information to make good decisions.

To investigate this question, we used similar Monte Carlo methods (described in the electronic supplementary material) to simulate two ideal observer models for estimation of the capture angle \( \theta_C^{\text{MGE}} \) that would maximize EG in each of the 12 conditions. The two models (referred to as the stochastic setting model and the exact setting model) differed in two respects. The exact setting model used the information about direction of motion \( v_\Omega \) on the last time step before occlusion to set the location of the catcher. Specifically, the catcher was always centred at the point where the dot would have emerged from behind the occluder if it had continued moving in direction \( v_\Omega \). In contrast, the stochastic setting model did not use \( v_\Omega \) (as was the case for our observers). Furthermore, the stochastic setting model took into account the observer’s uncertainty in setting the location of the catcher (figure 3), whereas in the exact setting model the observer’s setting uncertainty was 0. The stochastic setting model is therefore a more realistic, cognitively bounded [21] model of human performance, whereas the exact setting model corresponds to an upper bound on human performance.

For both models, we used a Monte Carlo approach similar to that described earlier (see electronic supplementary material) to recover probability profiles for each \( \theta_C \) in each condition. All profiles were monotonically increasing as expected. We then computed the \( \text{EG}(\theta_C) \) using equation (1.1) for both ideal observer models. The capture angle settings that would maximize EG for each condition were then obtained from:

\[ \theta_C^{\text{MGE}} = \arg \max_{\theta_C} \text{EG}(\theta_C). \]  

(3.4)

We verified computationally, for both models, that the resultant expected value curves were unimodal, so there is a single maximum expected gain (MEG) solution that determines the best capture angle to use. The expected value curve for the stochastic setting model is shown in figure 5a (unbroken curve). The value of \( \theta_C^{\text{MGE}} \) and the associated MEG for the exact setting model are also shown (dashed vertical and horizontal lines). The value of \( \theta_C^{\text{MGE}} \) for the stochastic setting model is indicated by an unbroken vertical black line. The mean capture angle \( \theta_C \) and EG for each of our five observers is also shown (grey circles), together with the average across observers (white circle, vertical grey line).

Clearly, our observers’ capture angle settings (both on average and for the most part individually) were larger than the solutions predicted by the exact setting model MEG solution. Consequently, human performance is considerably worse than this model. This is not surprising; as demonstrated earlier (and in the electronic supplementary material), our observers did not take into account the direction of dot movement on the final step before occlusion. However, in all 12 conditions, the average capture angle obtained across observers is remarkably close to the stochastic setting model MEG solution, with root mean square error over conditions of around 3°.

These findings are supported by the expected efficiency data. In figure 5b, we plot expected efficiency, calculated as the expected points scored for each observer based on their capture angle as a percentage of the points...
Figure 5. (a) Expected gain (EG) curves generated by multiplying the $p_C$ (shown in the electronic supplementary material, figure S3) by the points that would be scored for a successful catch at each capture angle. The maximum of each curve is marked by a black vertical line. This maximum corresponds to the setting of the occluder maximizing expected gain (MEG) in the corresponding experimental condition. Mean trial-by-trial EGs are plotted against mean capture angle for each observer, shown as grey circles (error bars denote 95% confidence intervals). The mean capture angle across observers is marked by a grey vertical line and the mean EG across observers for this capture angle is shown as a white circle. The dashed black lines correspond to the MEG predictions of the exact setting model (see text). (b) Expected efficiency for the observed capture angles in each of the 12 experimental conditions for each of the five observers individually and for the average over observers (avg). Error bars for each observer represent 95% confidence intervals, whereas error bars for the average observer are ± 1 s.e.
they could have scored using the MEG solution for the stochastic setting model. The expected efficiencies are high for all observers and stable across all conditions, indicating that observers were able to take the exogenous variability into account in making capture width settings. The mean efficiency (relative to the stochastic setting model) for the average observer across the conditions is significantly different from 1 and the 95% CI for \( \theta_C \) against the observed capture angles (parameter values arising from the fits are described in the text). Values for different occluder widths \( W \) are plotted in distinct symbols. \( W_O = 1 \) (circles), \( W_O = 2.5 \) (squares), \( W_O = 4 \) (triangles).

Figure 6. A plot of \( \hat{\theta}_C \) (the regressed capture angle obtained by regressing \( \hat{\theta}_C \) against the observed capture angles (parameter values arising from the fits are described in the text)). Values for different occluder widths \( W \) are plotted in distinct symbols. \( W_O = 1 \) (circles), \( W_O = 2.5 \) (squares), \( W_O = 4 \) (triangles).

The results regarding recovery of uncertainty information replicate and extend findings from Graf et al. [18], in which explicit estimation of visual motion variability was also addressed. The task given to observers in [18] was less well defined than the task used in the current study. In [18], observers were instructed to adjust the length of the (linear) catcher until it was at the smallest size for which they were ‘confident’ it would catch the dot. Clearly, this instruction is open to interpretation regarding what is meant by ‘confident’. Here, we avoid this problem by assigning a points reward for each catcher size and asking the observer to score as many points as possible. The observer’s winnings are an objective measure of how well they carried out the task. The points manipulation (together with the bonus prize given for scoring most points) had another benefit in that it is also likely to have increased motivation in the experiment. This was a further potential problem in the study of Graf et al. [18], where no feedback was given (the observer never saw the outcome of the extrapolation judgement).

The fact that we replicate the findings of Graf et al. [18] in the present experiment (in spite of these changes in methodology) provides compelling evidence that observers can recover an estimate of external motion variability that is tightly coupled to the actual variability in the exogenous source. This can be summarized in stating that human observers appear to know precisely how much more variable one path is than another.

The decision-making analysis undertaken indicated that observers are able to use the variability information recovered from the motion trajectory appropriately to inform decision-making about the size of the catcher. This is particularly evident when we take into account the noise in observer estimates of where the dot will emerge relative to the point at which it hit the inner edge of the occluder. In fact we found that, in this case, observer performance was very close to the MEG solution under the assumptions of a bounded model. Our work leaves open the question as to how observers carry out the task. How do they combine fallible visual estimates across the visible part of the object trajectory and use them to select a capture region? A full understanding of human visual and cognitive capabilities in such tasks requires that we go beyond measures of performance and develop plausible process models as well [22].

One possible outcome in any decision task is that changes in EG associated with even large changes in decision strategy may have negligible effect on the decision-maker’s winnings. If the EG function has a ‘flat maximum’ [23], then observers may exhibit biases in their settings that have little or no effect on their expected winnings. However, the observers’ settings in figure 5a are evenly distributed around the corresponding maxima, suggesting that observers were sensitive to the gradient of reward present. It is still possible that if we increased the reward values then their performance would improve even further, and consequently we regard our estimates of human ability to be conservative.

It is common in economic decision-making tasks that individual performance is best described using a model that incorporates biased representations of both value and probability [24]. Conversely, the fact that our observers’ performance was close to the (bounded) MEG solution suggests that they were able to use unbiased
representations of probability and value. How do we reconcile these results?

The first issue to consider here is that in the present experiment the probabilities are not provided explicitly in numerical forms. It may well be the case that decision-makers are biased in the representation of explicitly presented probabilities, but they are able to encode and use probability information appropriately when it is obtained more naturally via experience [25]. Second, in economic decision-making experiments, participants commonly make small numbers of ‘single shot’ decisions about large values. In contrast, in the present study, observers make many choices between small values. The representation of small values will naturally tend to be less biased, but also when making many choices economic decision makers tend to become less biased (closer to MEG) [26].

To conclude, we suggest that it is important for the visual system to be able to estimate the external variability in the movement of objects in the environment and use this information to aid in the choice between actions, which involve interaction with or avoidance of that object. When taken together with the results of studies that have examined ability to account for endogenous variability, this study suggests that human observers are finely tuned to uncertainty in general and can exploit this information to guide action.

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ENDNOTES

1 We use a polar coordinate system (r, θ) centred on the starting point.
2 The goodness-of-fit measure (r²) is a comparison between a fit with only a constant term and a fit with additional terms. Consequently, it is not defined for a regression without intercept.

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